Machine learning without human supervision on neuroscience data

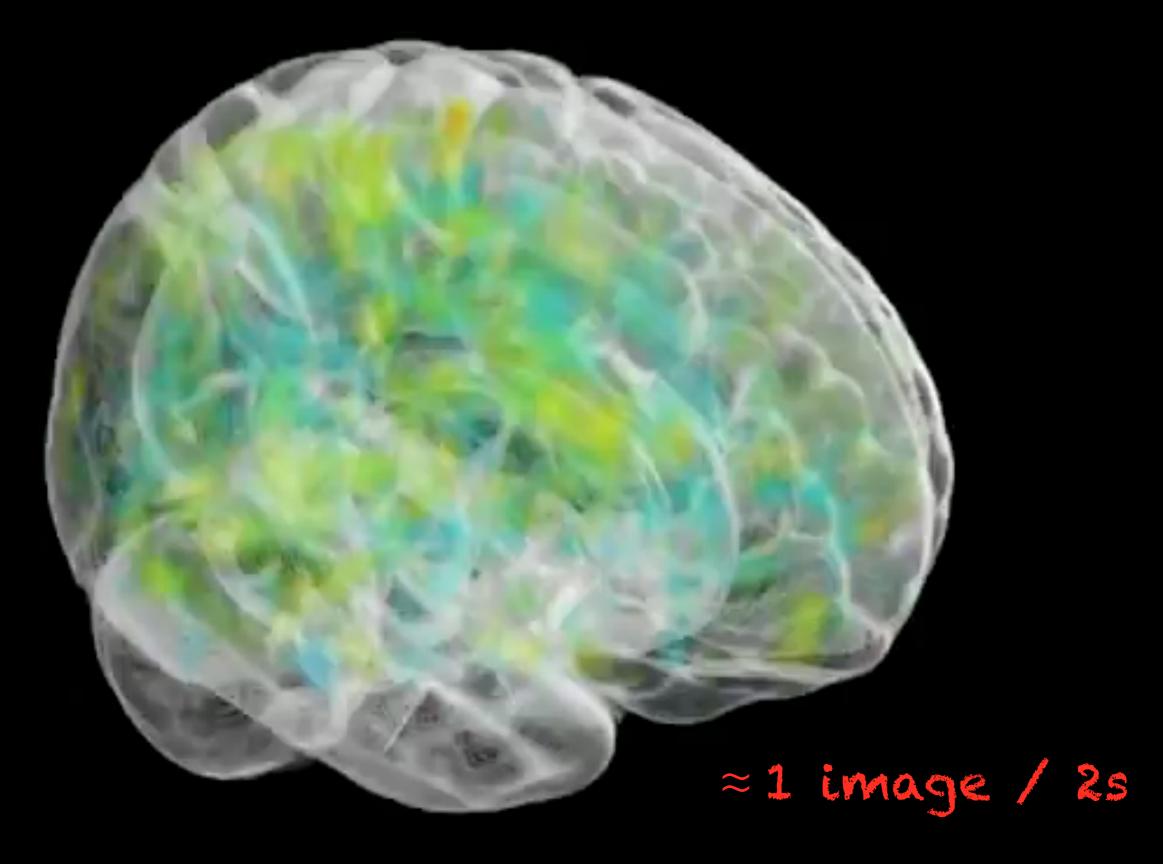
Alexandre Gramfort alexandre.gramfort@inria.fr http://alexandre.gramfort.net





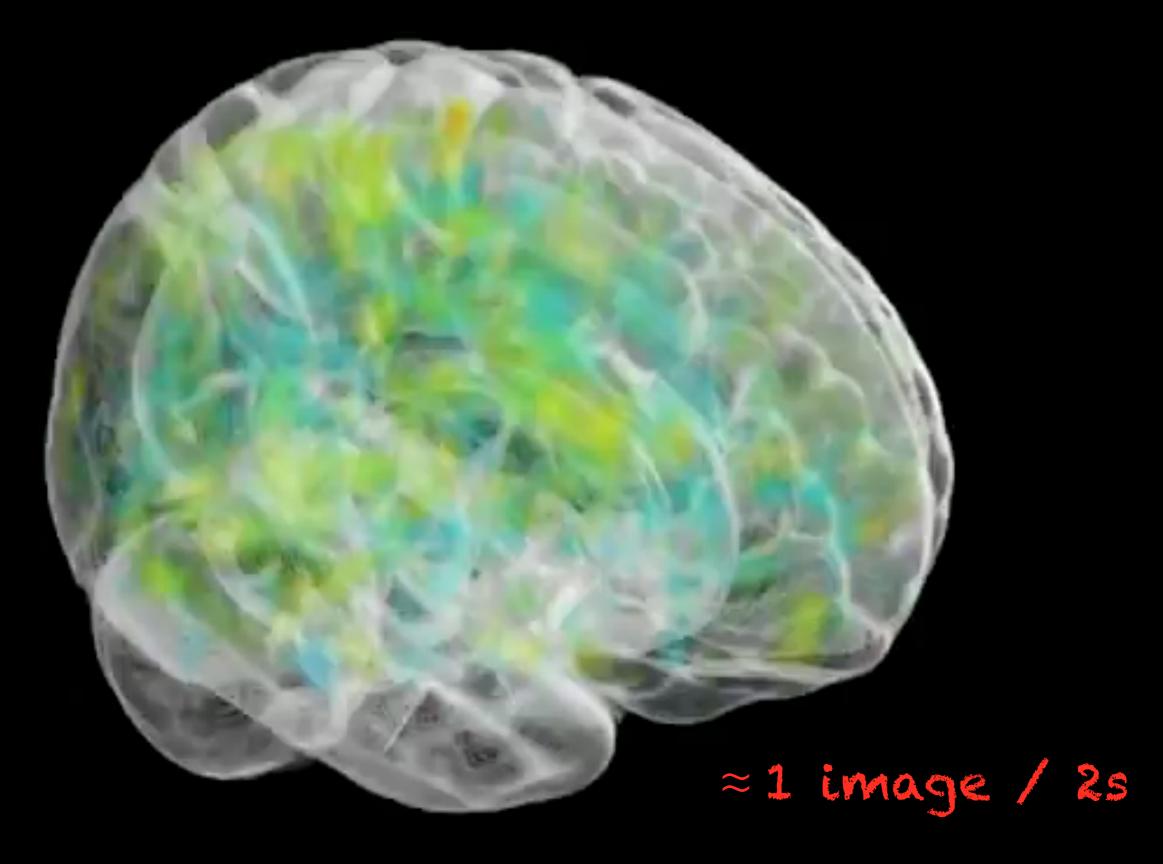
Nantes - June 2022

Functional MRI



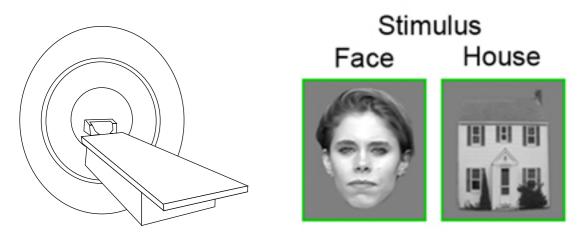
http://www.youtube.com/watch?v=uhCF-zlk0jY

Functional MRI

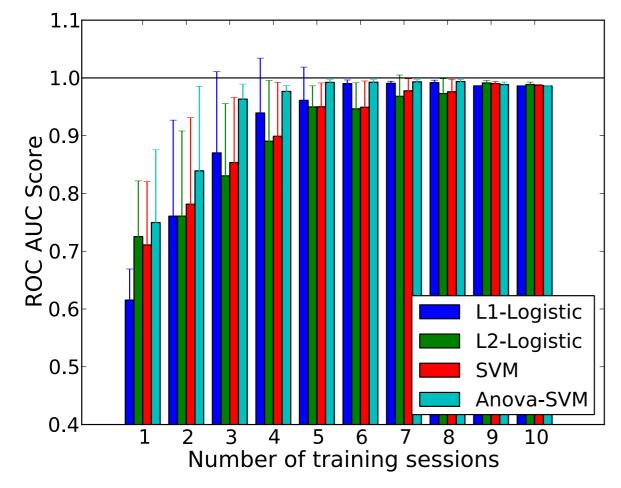


http://www.youtube.com/watch?v=uhCF-zlk0jY

Supervised Learning on fMRI: Face vs. House



Binary classification results



[Gramfort et al. 2011]

- The more data the better
- Almost no noise

It's often much harder:

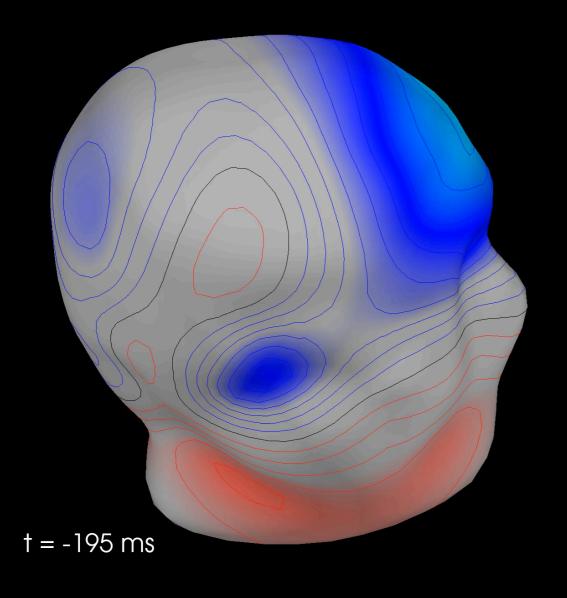
- Smaller effect sizes
- Intersubject variability
- Device variability etc.

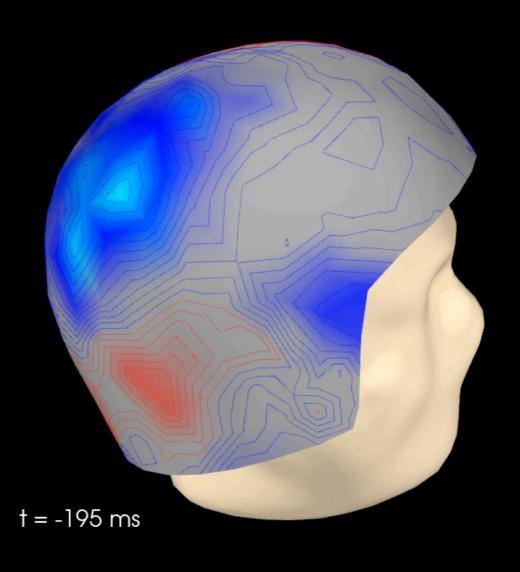


[Pedregosa, Varoquaux, Gramfort et al. JMLR 2011]

Electroencephalography (EEG) Electric Potential [V]

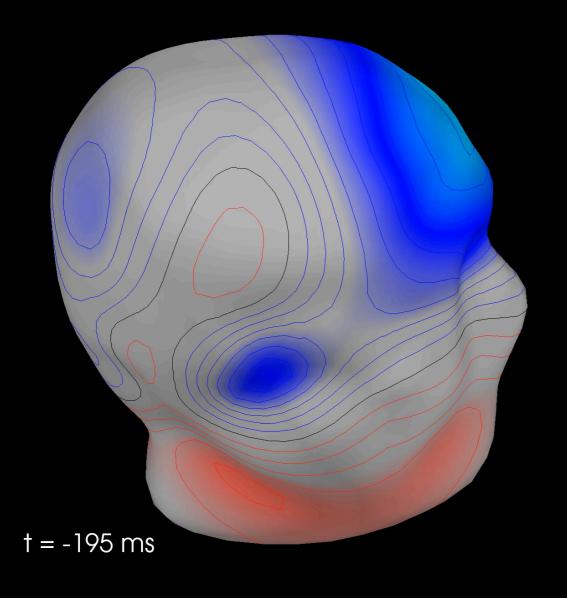
Magnetoencephalography (MEG) Magnetic field [T]

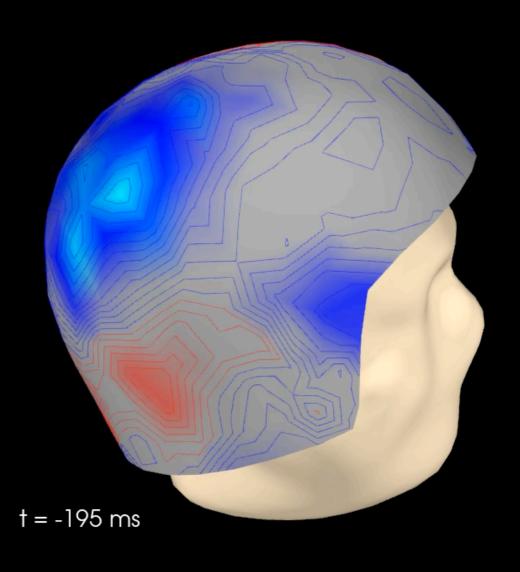




Electroencephalography (EEG) Electric Potential [V]

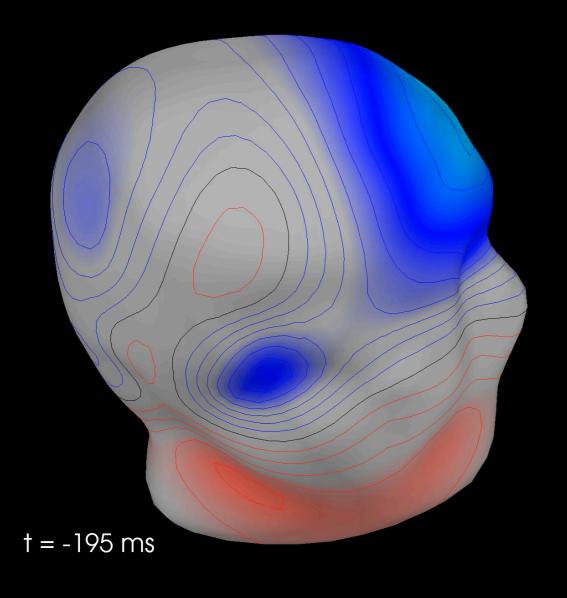
Magnetoencephalography (MEG) Magnetic field [T]

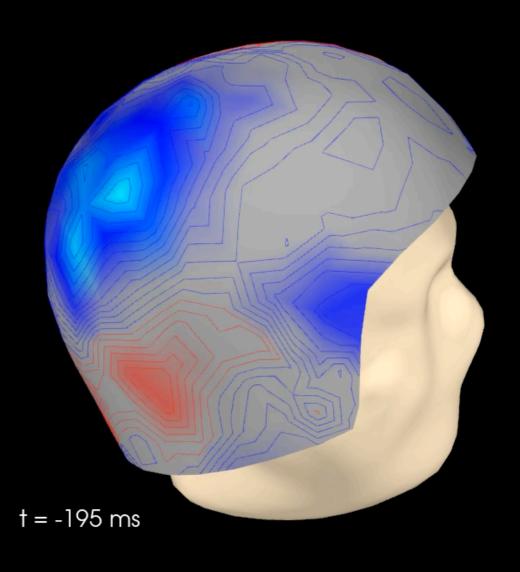




Electroencephalography (EEG) Electric Potential [V]

Magnetoencephalography (MEG) Magnetic field [T]





Outline: From unsupervised to self-supervised

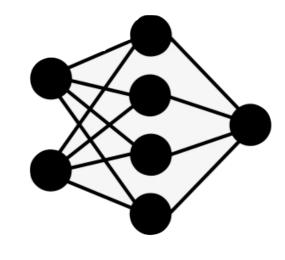
Unsupervised learning: From ICA to multiview ICA

P. Ablin, J-F Cardoso, A. Gramfort (2017), Faster independent component analysis by preconditioning with Hessian approximations, IEEE Trans. Sig. Proc.

H. Richard, L. Gresele, A. Hyvärinen, B. Thirion, A. Gramfort, P. Ablin (2020), Modeling Shared Responses in Neuroimaging Studies through MultiView ICA, Proc. NeurIPS

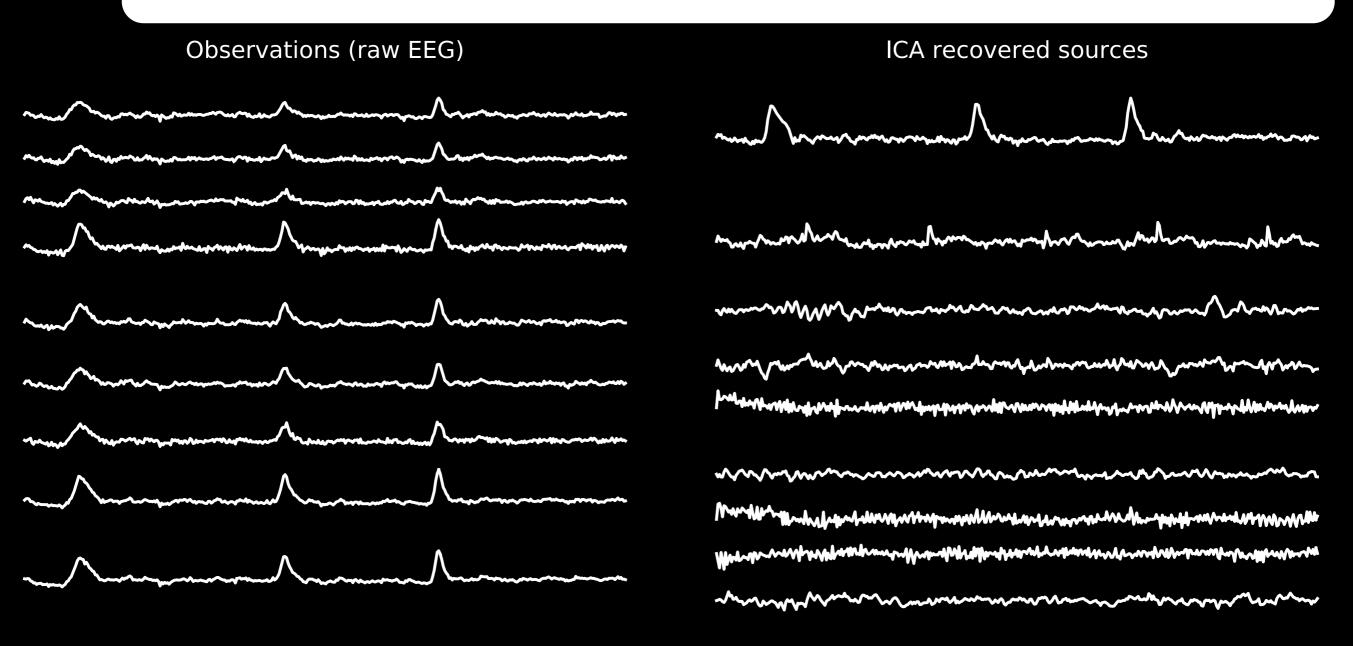
Self-supervised learning on EEG data

Banville, H., Chehab, O., Hyvärinen, A., Engemann, D. and Gramfort, A. (2020), Uncovering the structure of clinical EEG signals with self-supervised learning, Journal of Neural Engineering



1

From Independent Component Analysis (ICA) to multivew ICA

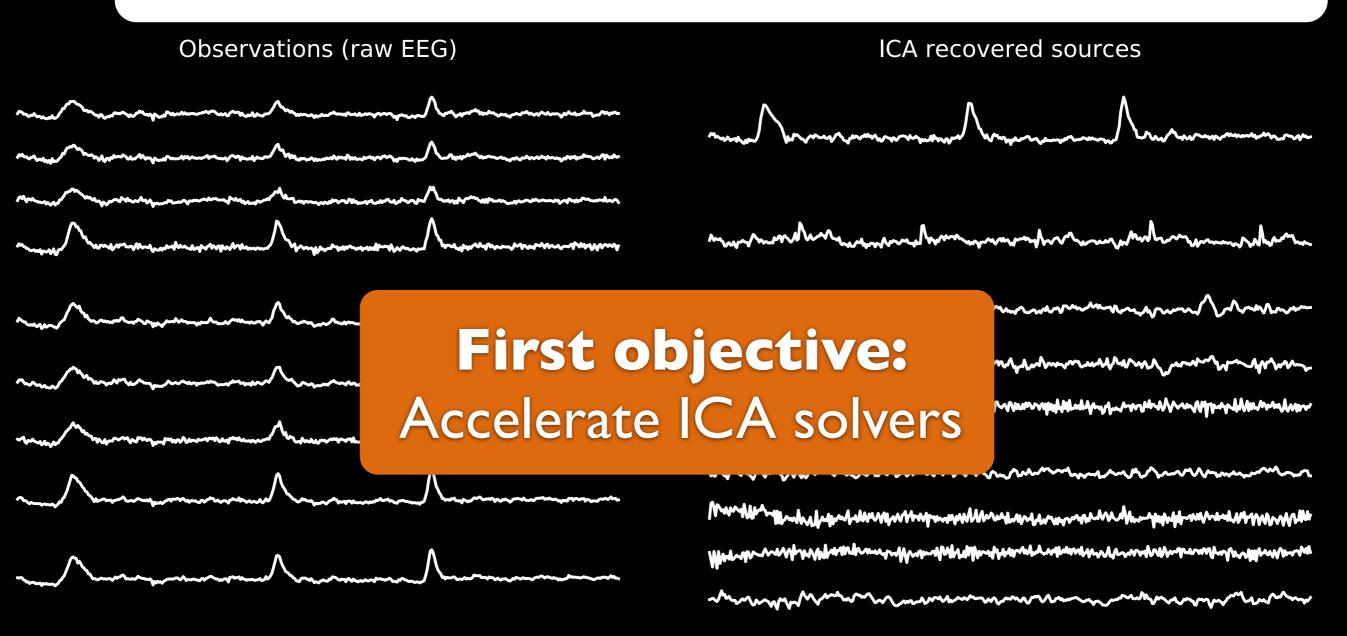


[Faster independent component analysis by preconditioning with Hessian approximations, P. Ablin, J.-F. Cardoso & A. Gramfort 2017 IEEE Trans. Signal Processing]

Code: https://pierreablin.github.io/picard

1

From Independent Component Analysis (ICA) to multivew ICA

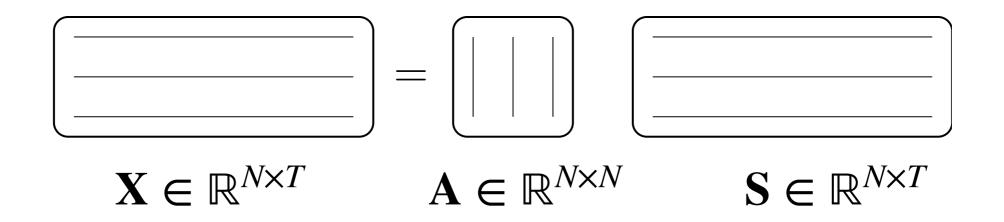


[Faster independent component analysis by preconditioning with Hessian approximations, P. Ablin, J.-F. Cardoso & A. Gramfort 2017 IEEE Trans. Signal Processing]

Code: https://pierreablin.github.io/picard

Linear ICA model: X = AS

 Assumption: Observed signals are a linear mix of independent identically distributed signals.



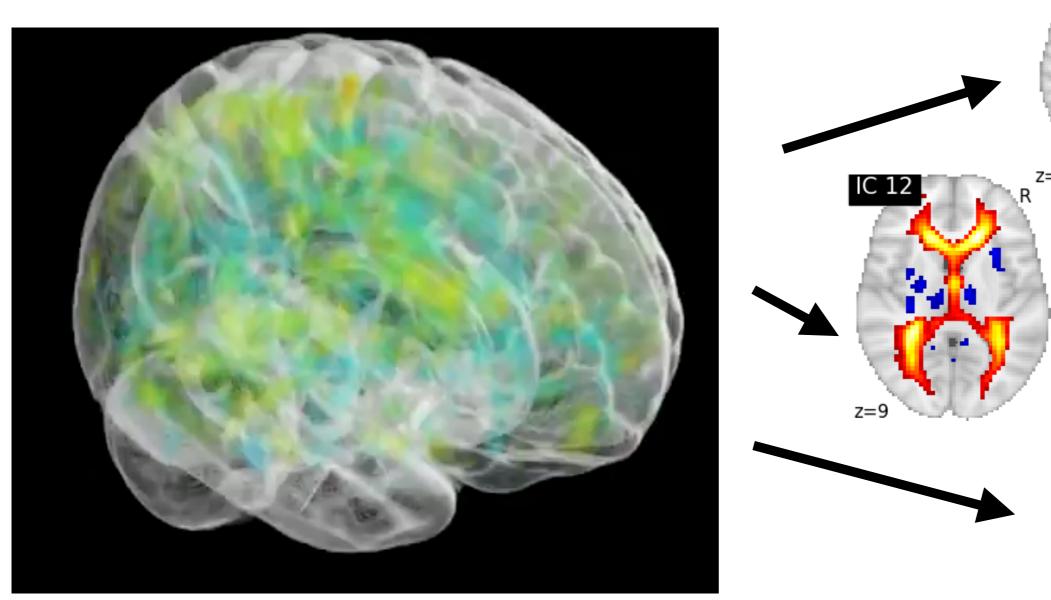
- N: Number of signals
- T: Number of samples
- X: Observed signals
- S: Independent sources signals
- A: Mixing matrix

Both A and S are unknown

[Jutten & Herault 91, Bell & Sejnowski 1995, Hyvärinen 1997]

Why should you care?

Used in neuroimaging to find "brain networks" (not neural networks...) in functional MRI data

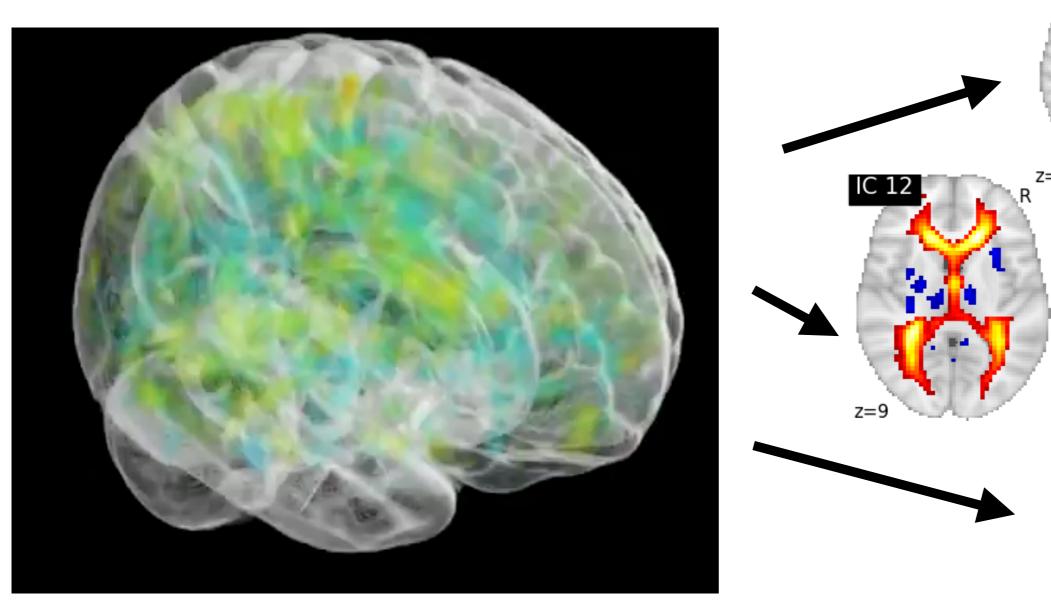


z=9

Source: http://nilearn.github.io/auto_examples/03_connectivity/plot_canica_resting_state.html

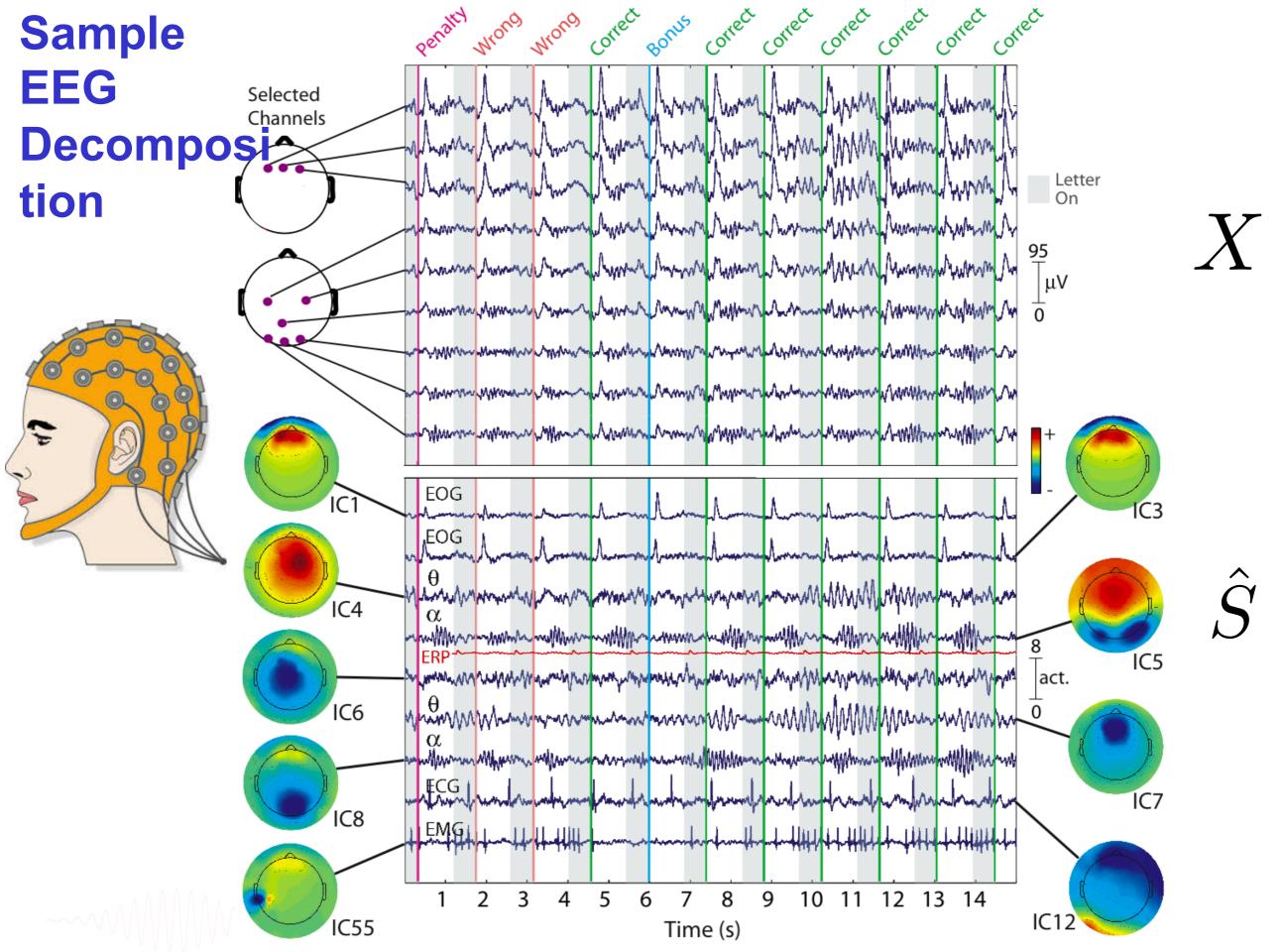
Why should you care?

Used in neuroimaging to find "brain networks" (not neural networks...) in functional MRI data



z=9

Source: http://nilearn.github.io/auto_examples/03_connectivity/plot_canica_resting_state.html



Source: EEGLAB software documentation

Principles of (non-Gaussian) ICA

$$X = AS$$

Objective: Find W s.t. WX has maximally independent rows.

Model: Let Y = WX denote the unmixed data

$$p(\mathbf{Y}(t)) = p_1(\mathbf{Y}_1(t)) \dots p_N(\mathbf{Y}_N(t))$$

Principles of (non-Gaussian) ICA

$$X = AS$$

Objective: Find W s.t. WX has maximally independent rows.

Model: Let Y = WX denote the unmixed data

$$p(\mathbf{Y}(t)) = p_1(\mathbf{Y}_1(t))...p_N(\mathbf{Y}_N(t))$$

Likelihood: With Y = g(X) = WX

$$p(\mathbf{X}) = p(g(\mathbf{X})) | \det J_{g(\mathbf{X})} | = p(\mathbf{Y}) | \det \mathbf{W} |$$

cf. RealNVP [Dinh et al. 2016]

Principles of (non-Gaussian) ICA

$$X = AS$$

Objective: Find W s.t. WX has maximally independent rows.

Model: Let Y = WX denote the unmixed data

$$p(\mathbf{Y}(t)) = p_1(\mathbf{Y}_1(t))...p_N(\mathbf{Y}_N(t))$$

Likelihood: With Y = g(X) = WX

$$p(\mathbf{X}) = p(g(\mathbf{X})) |\det J_{g(\mathbf{X})}| = p(\mathbf{Y}) |\det \mathbf{W}|$$

leads to:

cf. RealNVP [Dinh et al. 2016]

$$\mathcal{Z}(\mathbf{W}) = \log |\det \mathbf{W}| + \mathbb{E}_t \left(\sum_{i=1}^N \log p_i(\mathbf{Y}_i(t)) \right)$$

Optimization problem

$$\min_{\mathbf{W} \in \mathbb{R}^{N \times N}} -\log|\det \mathbf{W}| - \frac{1}{T} \sum_{t=1}^{T} \left(\sum_{i=1}^{N} \log p_i(\mathbf{Y}_i(t)) \right)$$

Optimization problem

$$\min_{\mathbf{W} \in \mathbb{R}^{N \times N}} -\log|\det \mathbf{W}| - \frac{1}{T} \sum_{t=1}^{T} \left(\sum_{i=1}^{N} \log p_i(\mathbf{Y}_i(t)) \right)$$

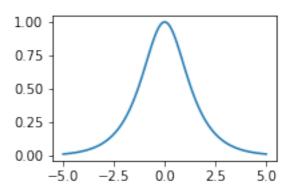
Infomax model [Bell & Sejnowski 1995]

Density $p_i(\,\cdot\,) \propto \frac{1}{\cosh(\,\cdot\,)}$

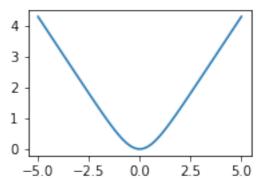
$$-\log(p_i(\,\cdot\,)) = \log(\cosh(\,\cdot\,)) + c$$

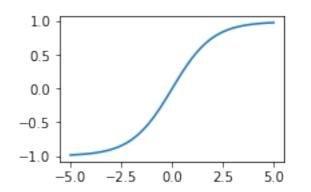
Score function:

$$\psi_i(\cdot) = -\log(p_i(\cdot))' = \tanh(\cdot/2)$$



Heavy-tail "sparse"





Geometry of the problem

- non-convex (multiple minima)
- Optimization on the invertible matrices manifold
- Use of a relative framework

Absolute

$$\mathbf{W}_{n+1} = \mathbf{W}_n + \delta \mathbf{W}$$

Relative

$$\mathbf{W}_{n+1} = (I_N + \delta \mathbf{W}) \mathbf{W}_n$$

Relative gradient / Hessian

Relative matrix form Taylor expansion:

$$\mathcal{L}((I+\mathcal{E})W) = \mathcal{L}(W) + \langle G|\mathcal{E}\rangle + \frac{1}{2}\langle \mathcal{E}|H|\mathcal{E}\rangle + \mathcal{O}(||\mathcal{E}||^3)$$

• Gradient is a $N \times N$ matrix:

$$G_{ij} = E[\psi_i(y_i)y_j] - \delta_{ij}$$

simple expressions

• Hessian is a $N \times N \times N \times N$ Fourth order tensor.

$$H_{ijkl} = \delta_{il}\delta_{jk} + \delta_{ik}E[\psi_i'(y_i)y_jy_l]$$

(relative) Newton method

$$H_{ijkl} = \delta_{il}\delta_{jk} + \delta_{ik}E[\psi_i'(y_i)y_jy_l]$$

One iteration:
$$W_{n+1} = (I - H^{-1}G)W_n$$

Problem:

Large linear system / regularization needed

Newton method is possible but not practical

(relative) Newton method

$$H_{ijkl} = \delta_{il}\delta_{jk} + \delta_{ik}E[\psi_i'(y_i)y_jy_l]$$

One iteration:
$$W_{n+1} = (I - H^{-1}G)W_n$$

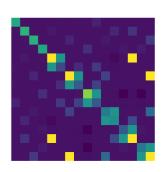
Problem:

Large linear system / regularization needed

Newton method is possible but not practical

but if model holds:

$$\delta_{ik}E[\psi_i'(y_i)y_jy_l] = \delta_{ik}\delta_{jl}E[\psi_i'(y_i)]E[y_j^2]$$



(relative) Newton method

$$H_{ijkl} = \delta_{il}\delta_{jk} + \delta_{ik}E[\psi_i'(y_i)y_jy_l]$$

One iteration:
$$W_{n+1} = (I - H^{-1}G)W_n$$

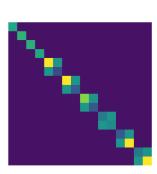
Problem:

Large linear system / regularization needed

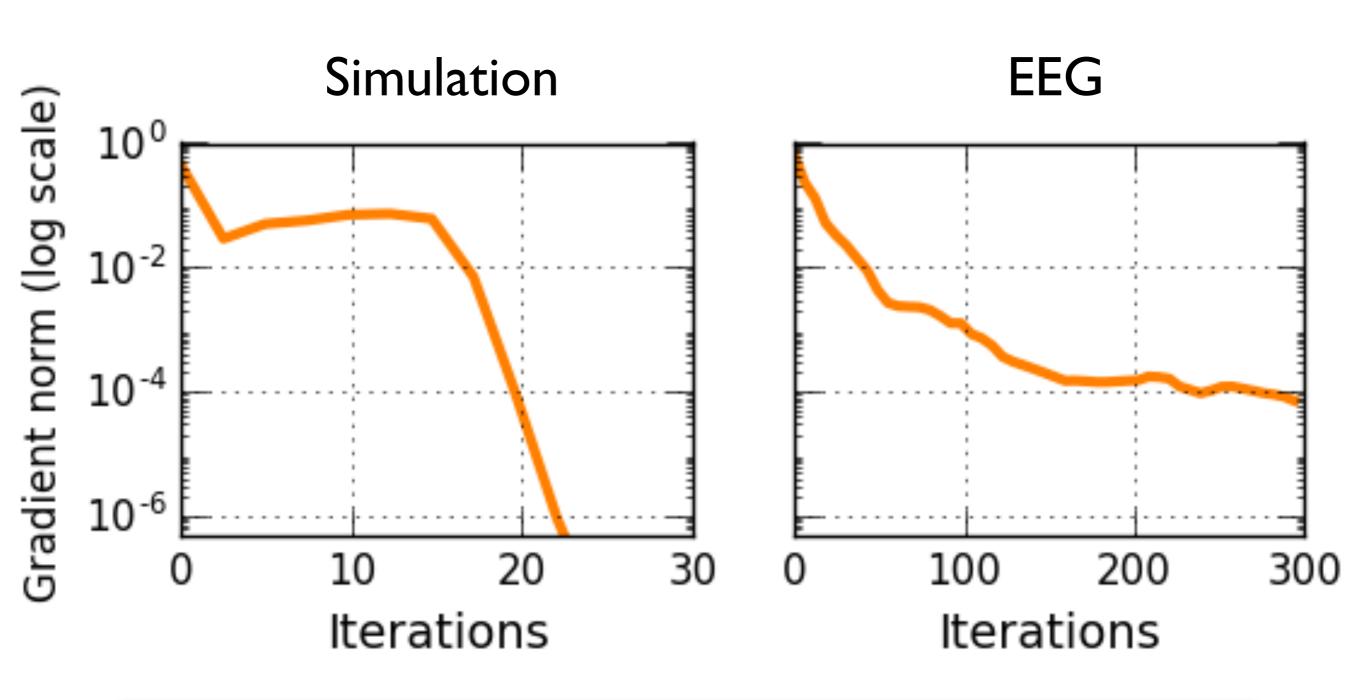
Newton method is possible but not practical

but if model holds:

$$\delta_{ik} E[\psi_i'(y_i)y_jy_l] = \delta_{ik}\delta_{jl} E[\psi_i'(y_i)]E[y_j^2]$$



But...



It does not work with real data!

L-BFGS algorithm with Hessian approx.

Idea:

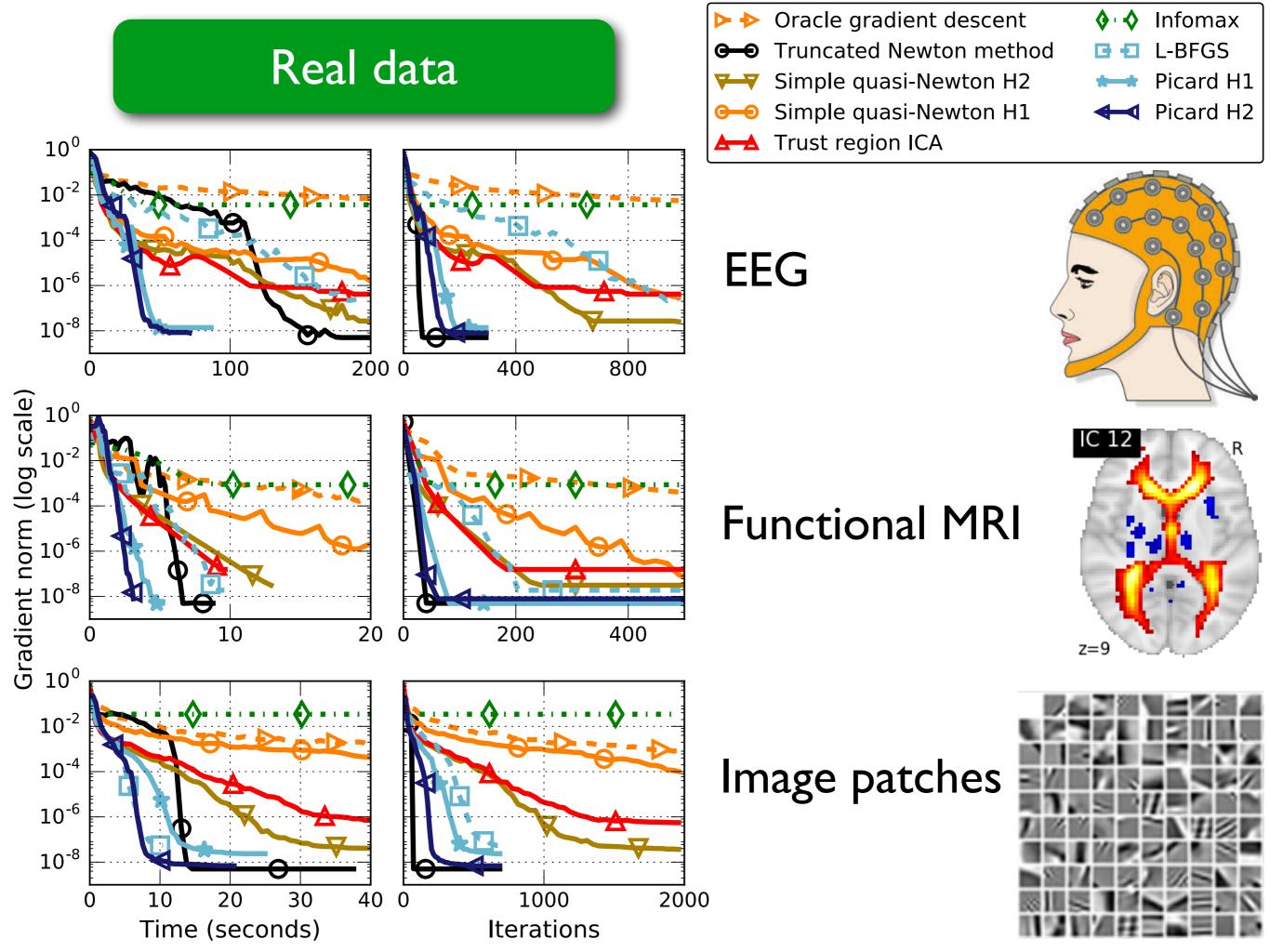
- Combine L-BFGS with Hessian approx.
- Replace diagonal initial guess by Hessian approx.
- The rest is the same (although written with relative gradients)...



[Liu, D. C., & Nocedal, J. « On the limited memory BFGS method for large scale optimization. » Mathematical programming, 1989]

[P.Ablin, J.-F. Cardoso, A. Gramfort,

Faster ICA by preconditioning with Hessian approximations, IEEE TSP 2017]



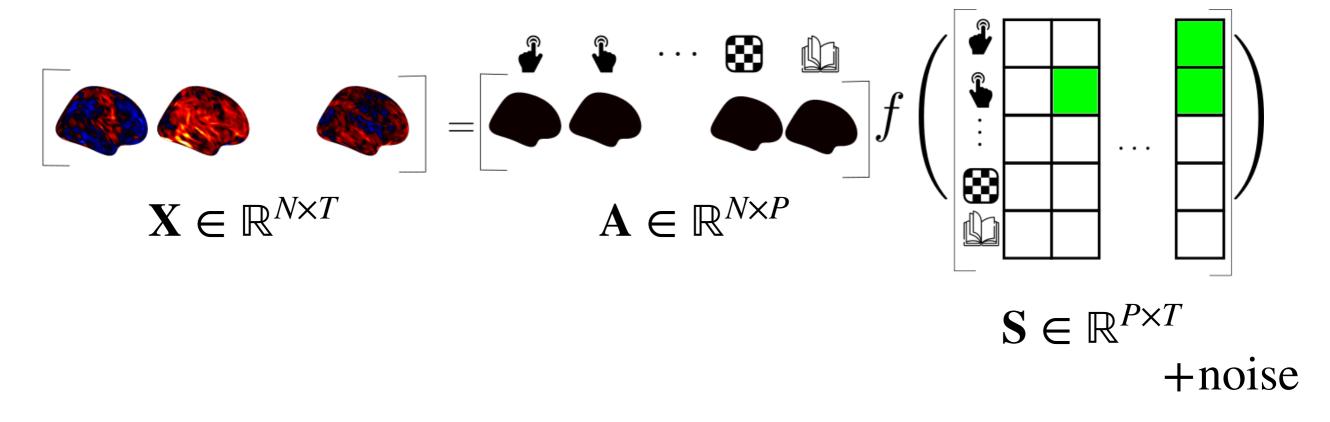
What if you have multiple sets X, e.g. from a population? Multiview ICA

[Modeling Shared Responses in Neuroimaging Studies through MultiView ICA Richard, H., Gresele, L., Hyvärinen, A., Thirion, B., Gramfort, A., Ablin, P. (2020). Proc. NeurIPS]

[Shared Independent Component Analysis for Multi-Subject Neuroimaging Richard, H., Ablin, P., Thirion, B., Gramfort, A., Hyvärinen, A. (2021). Proc. NeurIPS]

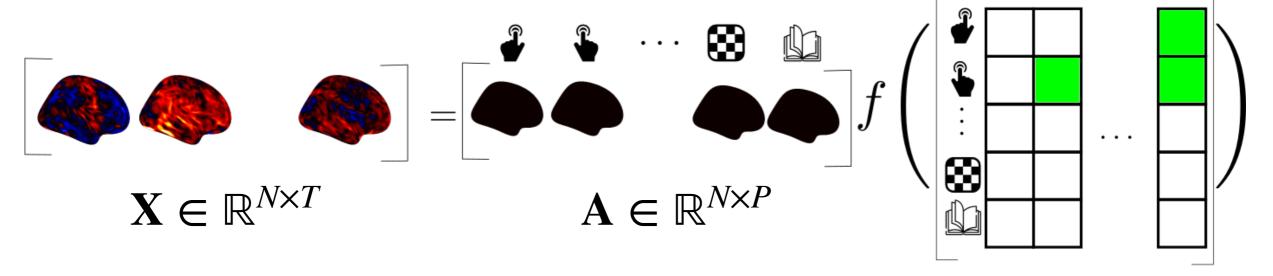
Towards naturalistic stimuli

Controlled stimuli

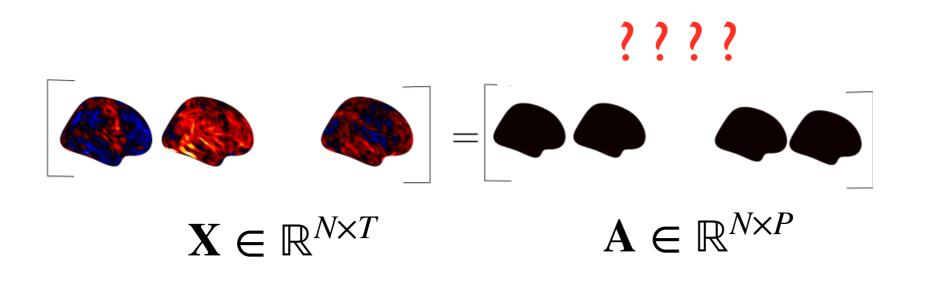


Towards naturalistic stimuli

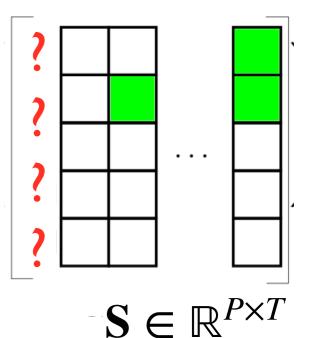
Controlled stimuli



vs. naturalistic stimuli (movies)



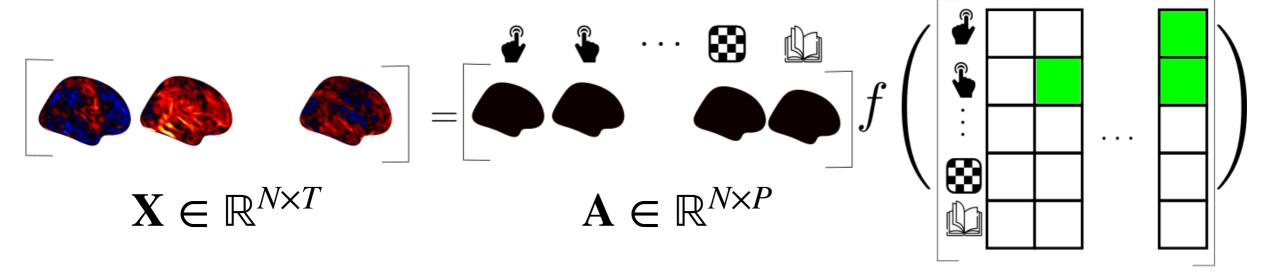
$$\mathbf{S} \in \mathbb{R}^{P \times T}$$
 +noise



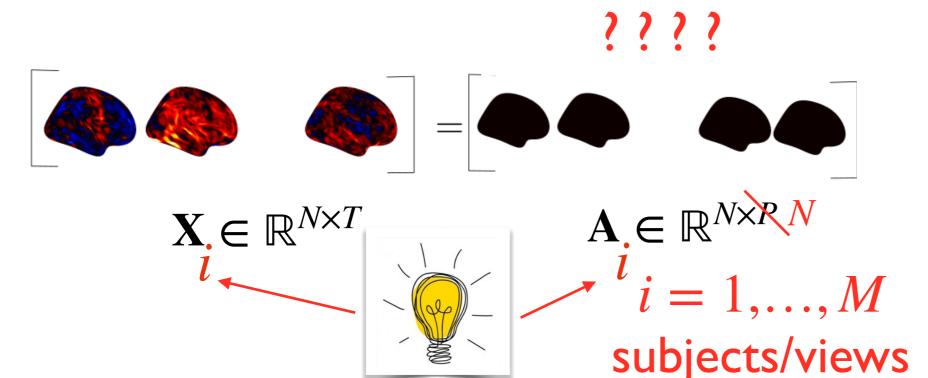
$$\mathbf{S} \in \mathbb{R}^{P \times T}$$
 +noise

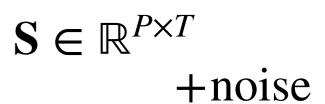
Towards naturalistic stimuli

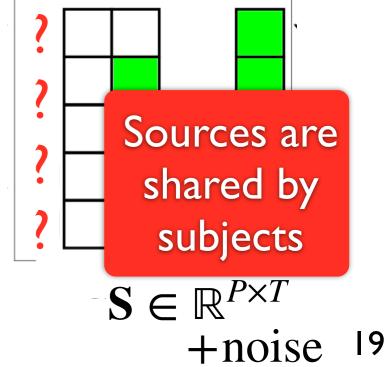
Controlled stimuli



vs. naturalistic stimuli (movies)







Multiview ICA

Model:
$$X^i = A^i(S + N^i)$$
, $i = 1,...,M$ X^i Data for subject i

Assumptions:

density as in Infomax (1/cosh)

Source independence:
$$p(\mathbf{S}(t)) = q(\mathbf{S}_1(t))...q(\mathbf{S}_N(t))$$

Gaussian noise:
$$\mathbf{N}_{j}^{i}(t) \sim \mathcal{N}(0,\sigma^{2})$$
 indefined

independent across components and independent from sources

Multiview ICA

Model:
$$\mathbf{X}^i = \mathbf{A}^i(\mathbf{S} + \mathbf{N}^i), i = 1,...,M$$
 \mathbf{X}^i Data for subject i

Assumptions:

density as in Infomax (1/cosh)

Source independence:
$$p(\mathbf{S}(t)) = q(\mathbf{S}_1(t)) \dots q(\mathbf{S}_N(t))$$

Gaussian noise: $N_i^i(t) \sim \mathcal{N}(0, \sigma^2)$

independent across components and independent from sources

$$\mathcal{L}(\mathbf{W}^i) = -\sum_{i=1}^{M} \log|\det \mathbf{W}^i| + f(\tilde{\mathbf{S}}) + \frac{1}{2\sigma^2} \sum_{i=1}^{M} \frac{\|\mathbf{W}^i \mathbf{X}^i - \tilde{\mathbf{S}}\|^2}{\text{"Error term"}}$$

Wⁱ Unmixing matrix for subject
$$i$$
 $\tilde{\mathbf{S}} = \frac{1}{M} \sum_{i=1}^{M} \mathbf{W}^{i} \mathbf{X}^{i}$ $f(\mathbf{S}) = \sum_{i=1}^{N} f(\mathbf{S}_{j})$

$$\tilde{\mathbf{S}} = \frac{1}{M} \sum_{i=1}^{M} \mathbf{W}^{i} \mathbf{X}^{i}$$

$$f(\mathbf{S}) = \sum_{j=1}^{N} f(\mathbf{S}_j)$$

$$f(\mathbf{S}_j) = \int \exp\left(-\frac{1}{2\sigma^2}Mz^2\right) q(\mathbf{S}_j - z)dz$$

Smoothed density

Optimization (same recipe)

Objective: Minimize the negative log-likelihood \mathscr{L} using a block-coordinate Newton descent

$$\mathbf{W}^i = (\mathbf{I} + \rho \mathbf{D}^i) \mathbf{W}^i$$

Multiplicative updates

$$\mathbf{D}^i = -(\tilde{\mathbf{H}}^i)^{-1}\mathbf{G}^i$$

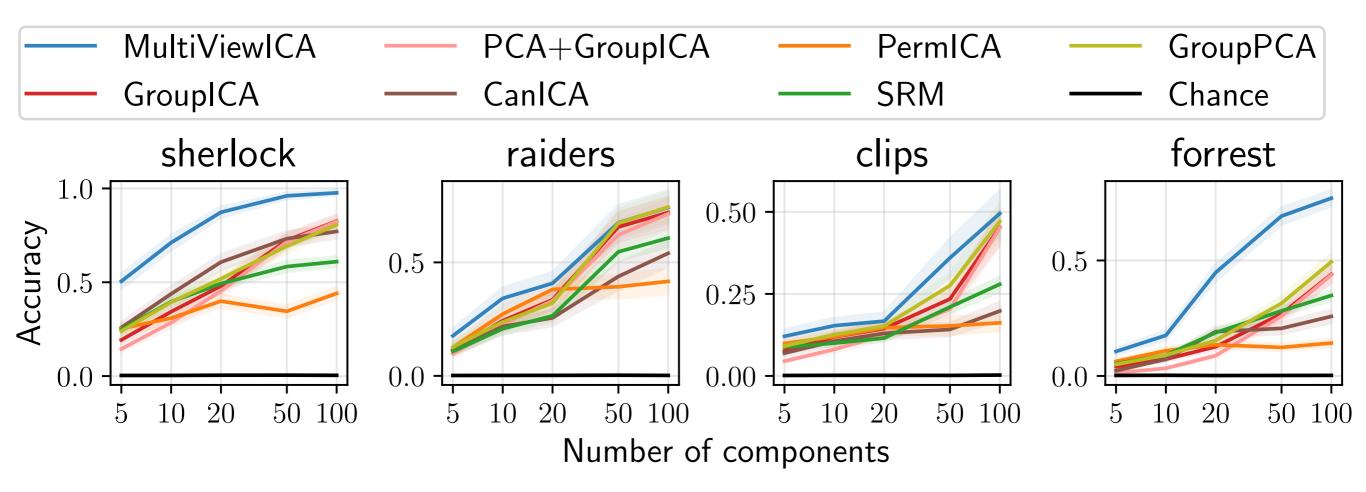
Relative "Newton descent" direction

$$\tilde{\mathbf{H}}^i$$

Sparse Hessian $(N \times N \times N \times N)$ Approximation with N^2 non-zeros

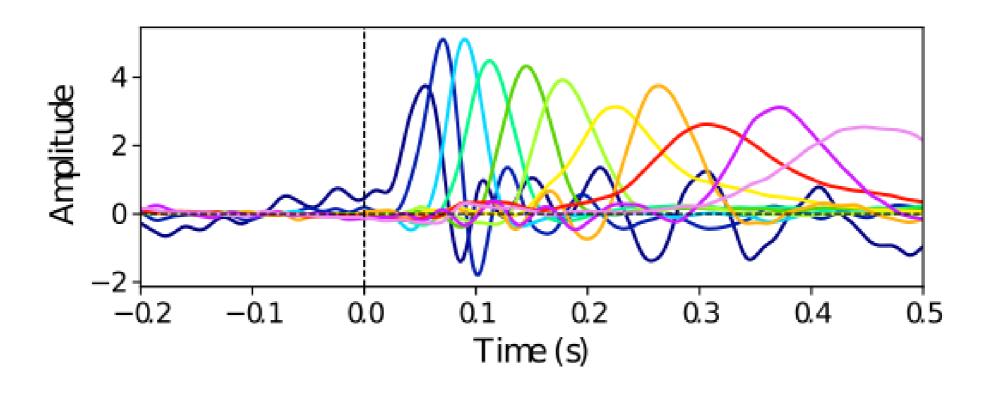
fMRI time segment matching

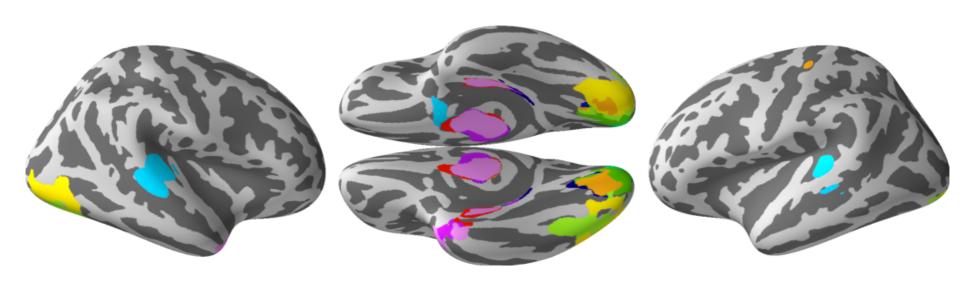
We select a target time-segment (9 consecutive timeframes) in the shared responses and try to localize the corresponding time-segment in the sources of the left-out subject using a maximum-correlation classifier



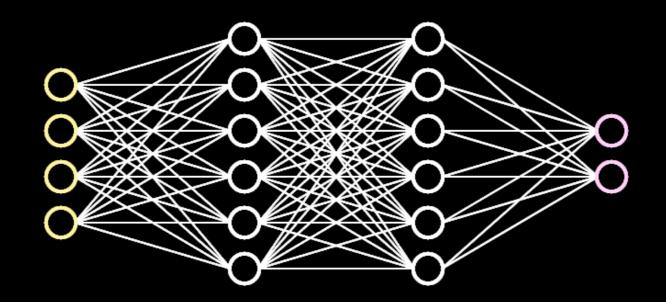
Experiment on MEG data

MEG data from Cam-CAN dataset with 200 subjects attending to audiovisual stimuli





Self-supervised learning on EEG



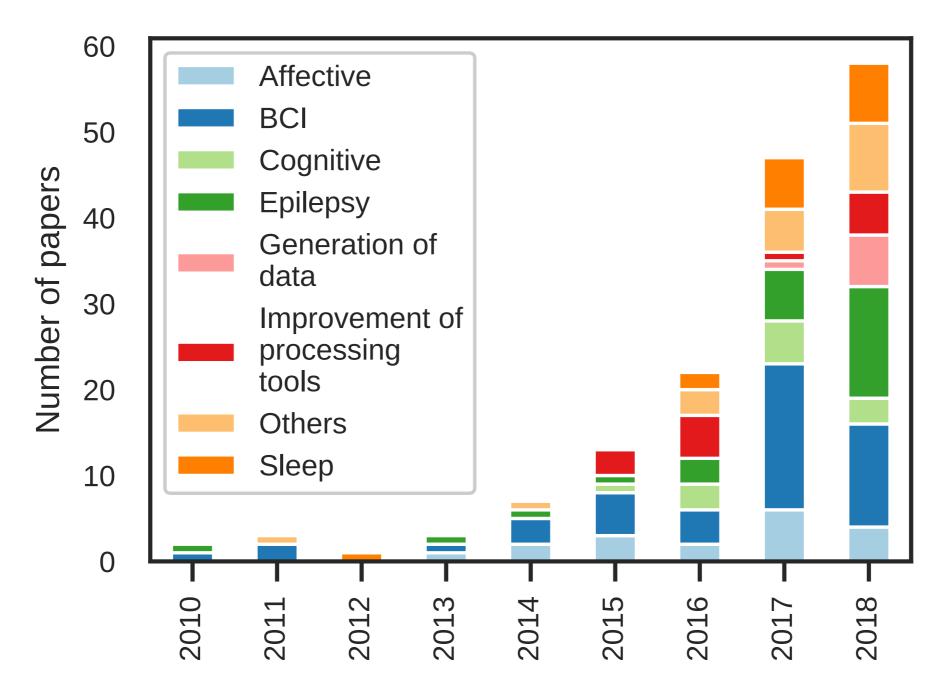
Uncovering the structure of clinical EEG signals with self-supervised learning Banville, H., Chehab, O., Hyvärinen, A., Engemann, D. and Gramfort, A. (2020)

Journal of Neural Engineering & ArXiv abs/2007.16104

Self-supervised representation learning from electroencephalography signals Banville, H., Albuquerque, I., Moffat, G., Engemann, D. and Gramfort, A. (2019)

Proc. Machine Learning for Signal Processing (MLSP).

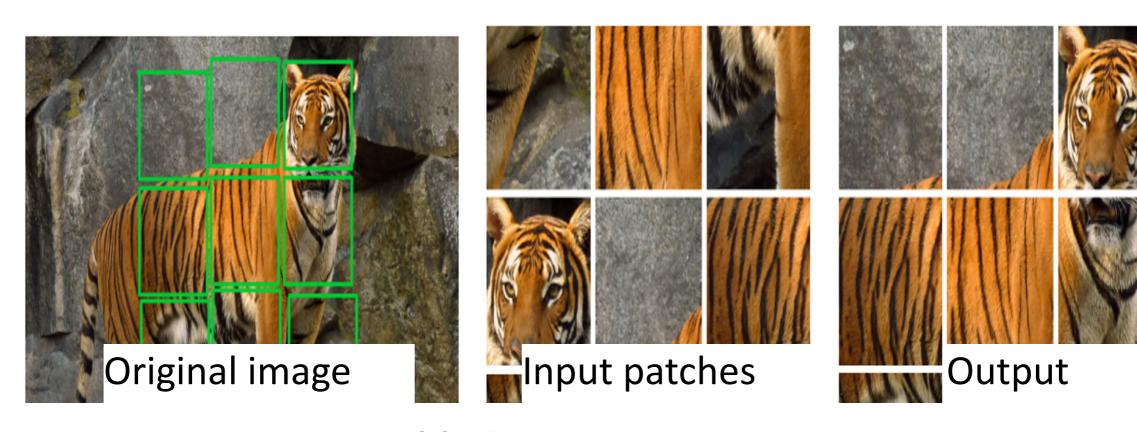
Deep Learning papers on EEG



[Deep learning-based electroencephalography analysis: a systematic review Roy, Y., Banville, H., Albuquerque, I., Gramfort, A., Falk, T. and Faubert, J. (2019)

Journal of Neural Engineering 16: (051001).]

Self-supervision

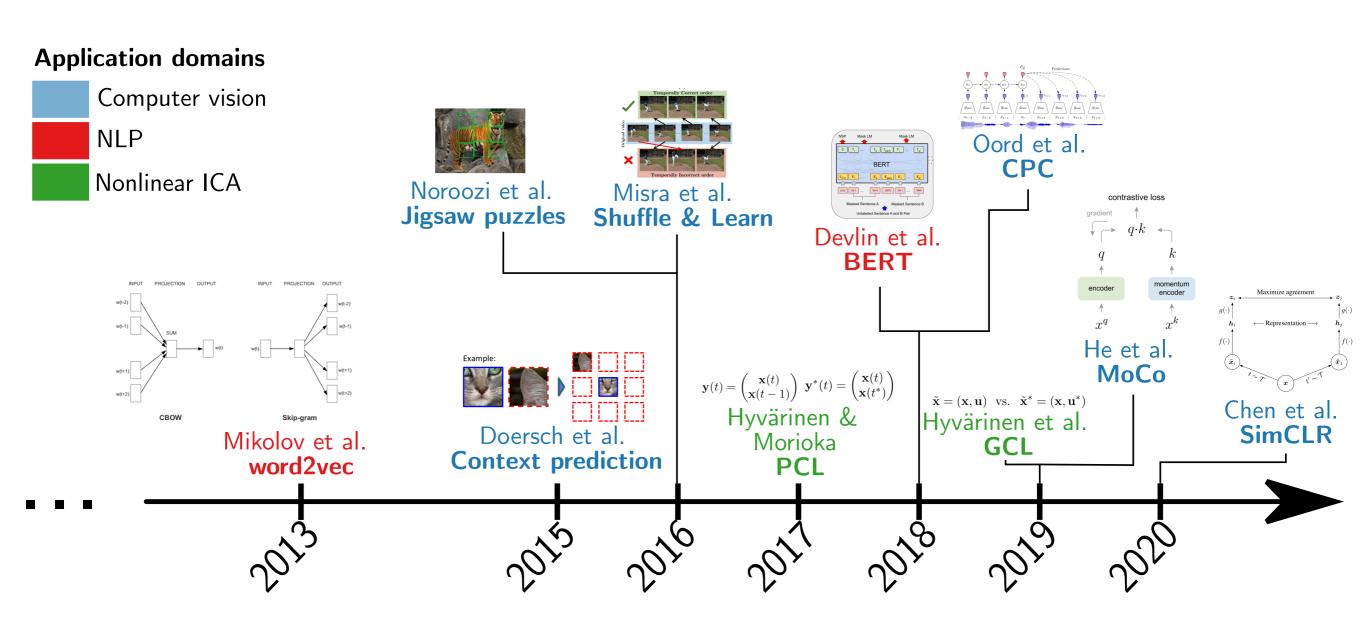


[Noroozi & Favaro 2016] use a deep neural network to solve the Jigsaw puzzle



Use the **structure** of the data to pretrain a **feature extractor** with a supervised *pretext task* – then use the features on a *downstream task*.

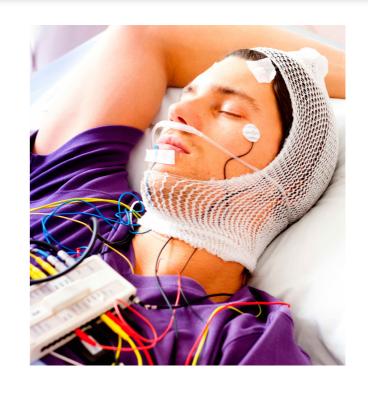
(Partial) History of SSL beyond EEG



Remarks: Heavily based on contrastive learning and possibly data augmentation techniques

Polysomnography (PSG)

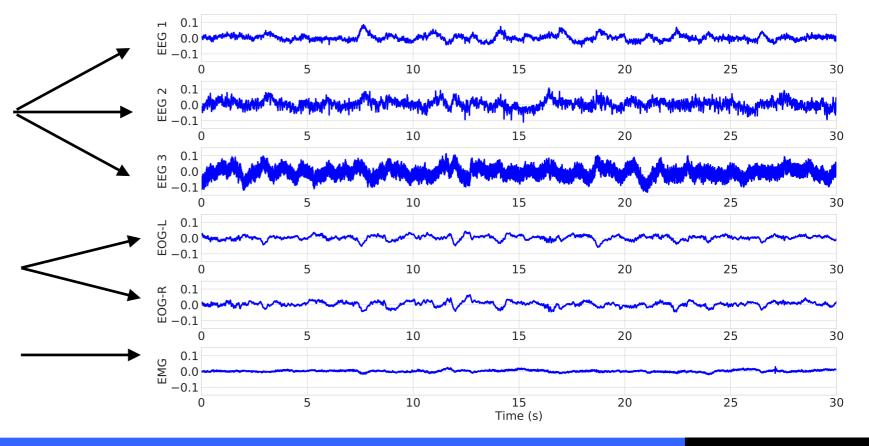
- Clinical exam
- Electrophysiological signals



Electro-encephalography (EEG)

Electro-oculography (EOG)

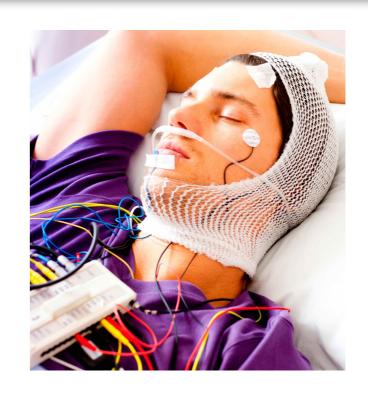
Electro-myography (EMG)



Polysomnography (PSG)

- Clinical exam
- Electrophysiological signals

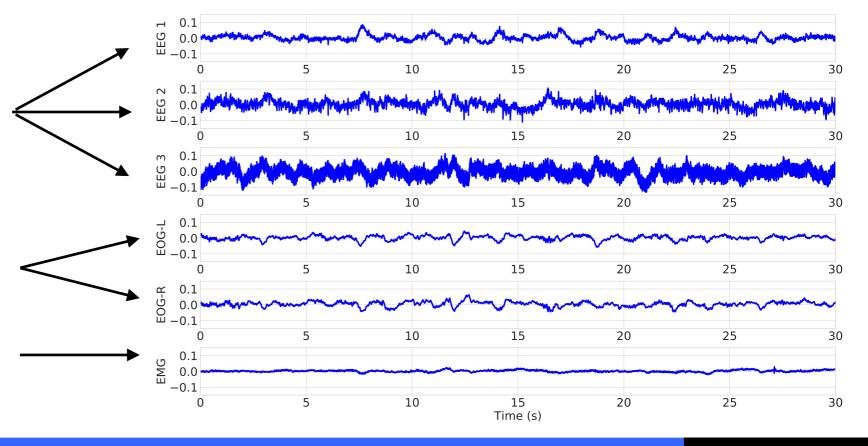
Routinely annotated by sleep experts



Electro-encephalography (EEG)

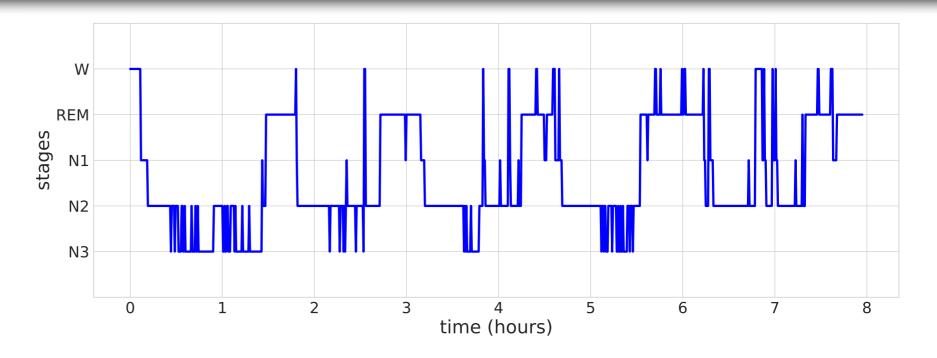
Electro-oculography (EOG)

Electro-myography (EMG)



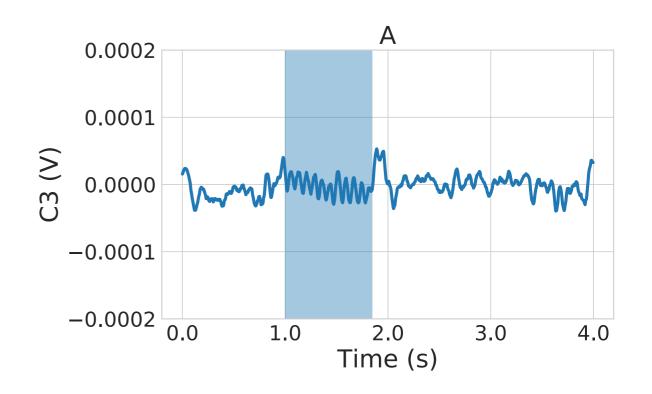
2 types of annotations

Hypnogram of sleep stages



[S. Chambon et al. (2018), IEEE Trans. Neural Systems and Rehabilitation Engineering]

Micro-events: Spindles, K-complex etc.

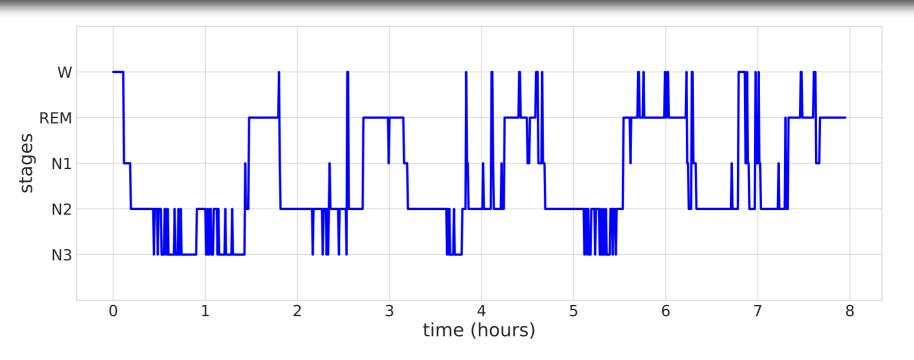


[S. Chambon et al. (2018), J. of Neuroscience Methods]

2 types of annotations

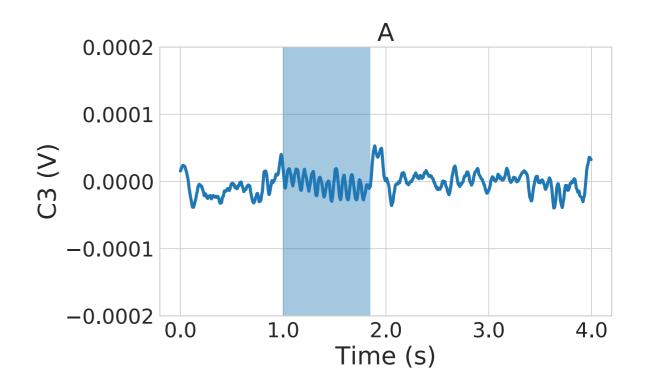
Hypnogram of sleep stages

Classification problem



[S. Chambon et al. (2018), IEEE Trans. Neural Systems and Rehabilitation Engineering]

Micro-events: Spindles, K-complex etc.

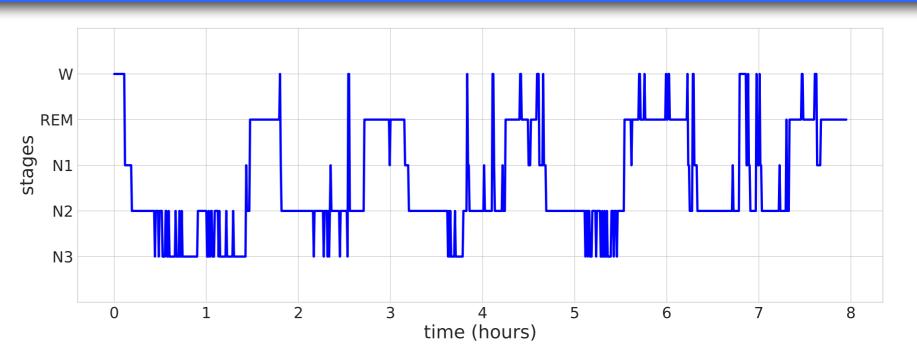


[S. Chambon et al. (2018), J. of Neuroscience Methods]

2 types of annotations

Hypnogram of sleep stages

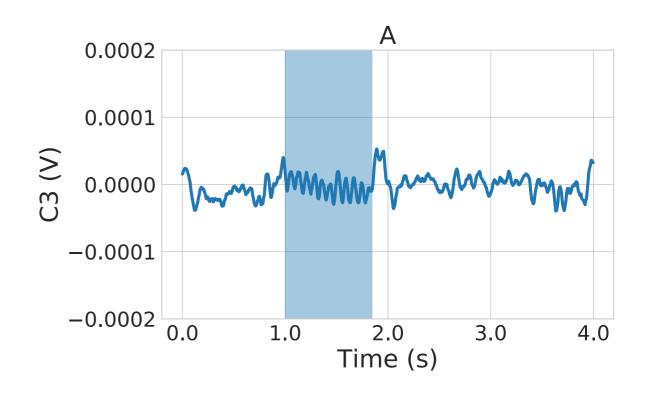
Classification problem



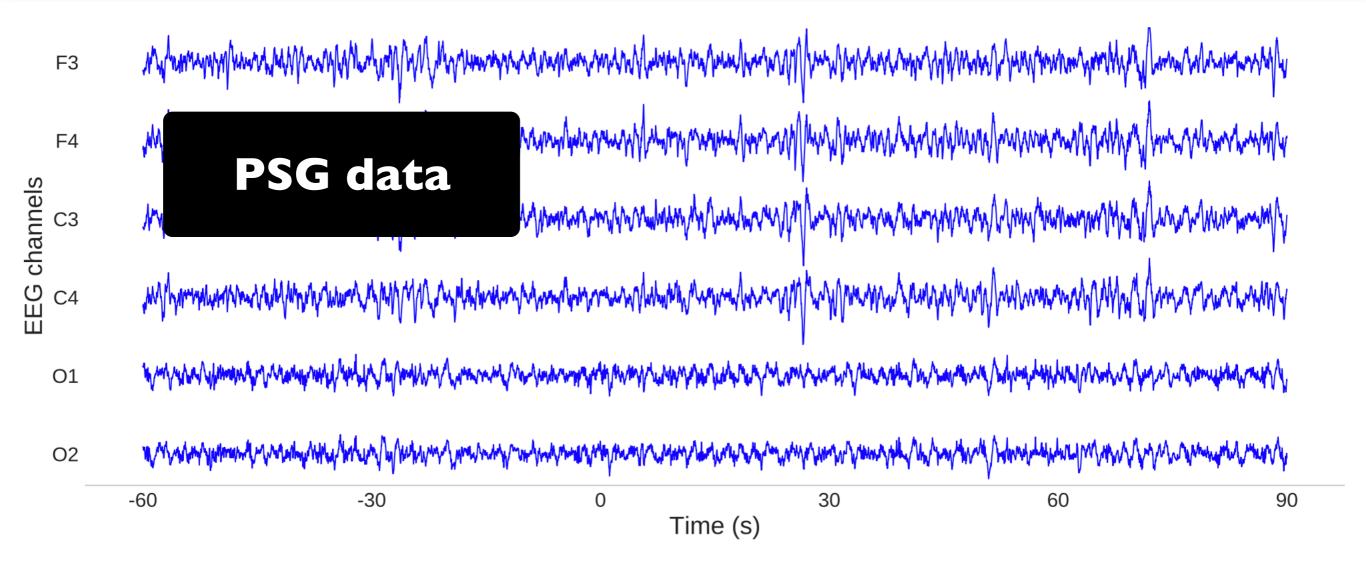
[S. Chambon et al. (2018), IEEE Trans. Neural Systems and Rehabilitation Engineering]

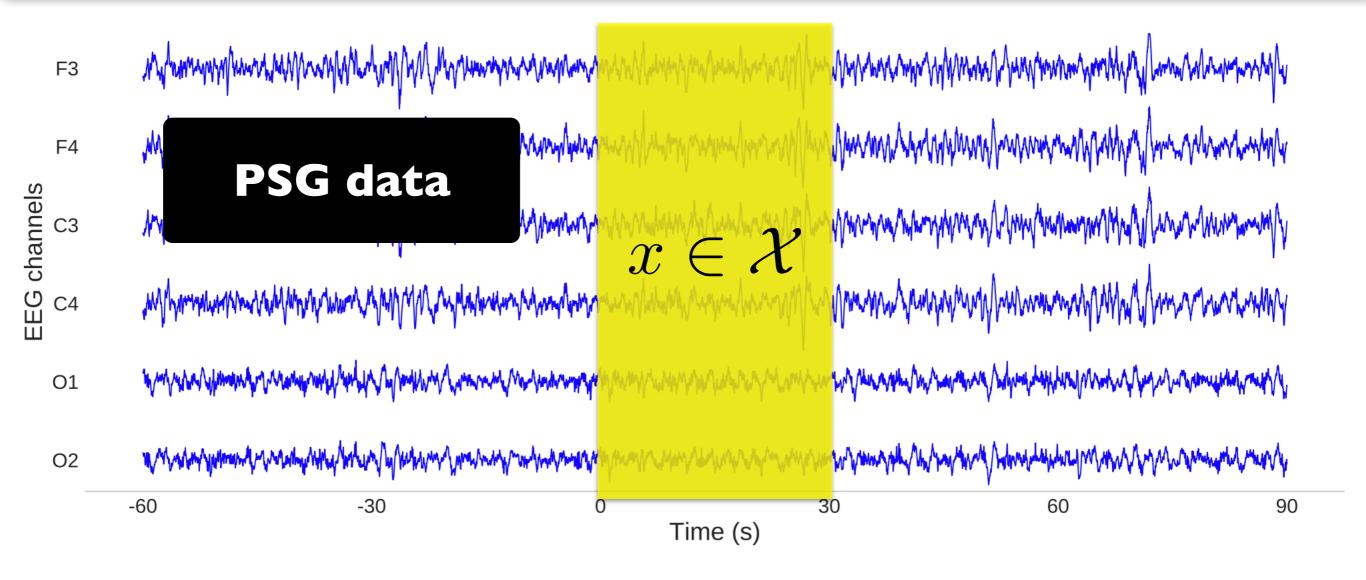
Micro-events: Spindles, K-complex etc.

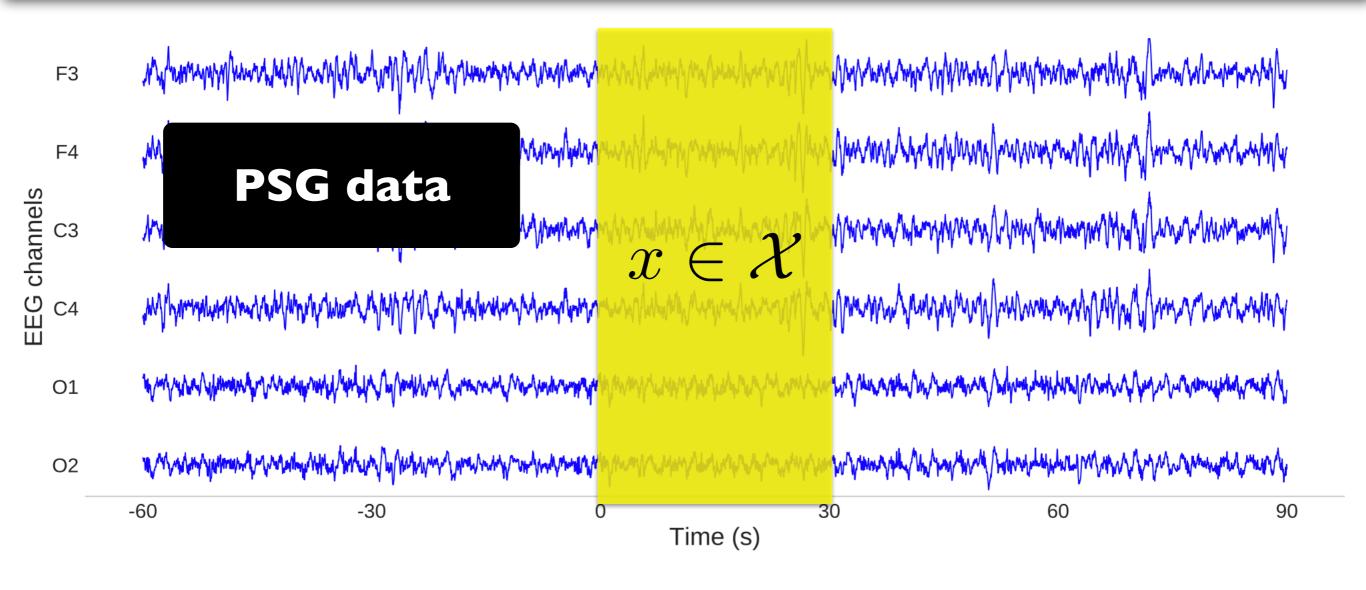
Joint detection and classification problem



[S. Chambon et al. (2018), J. of Neuroscience Methods]

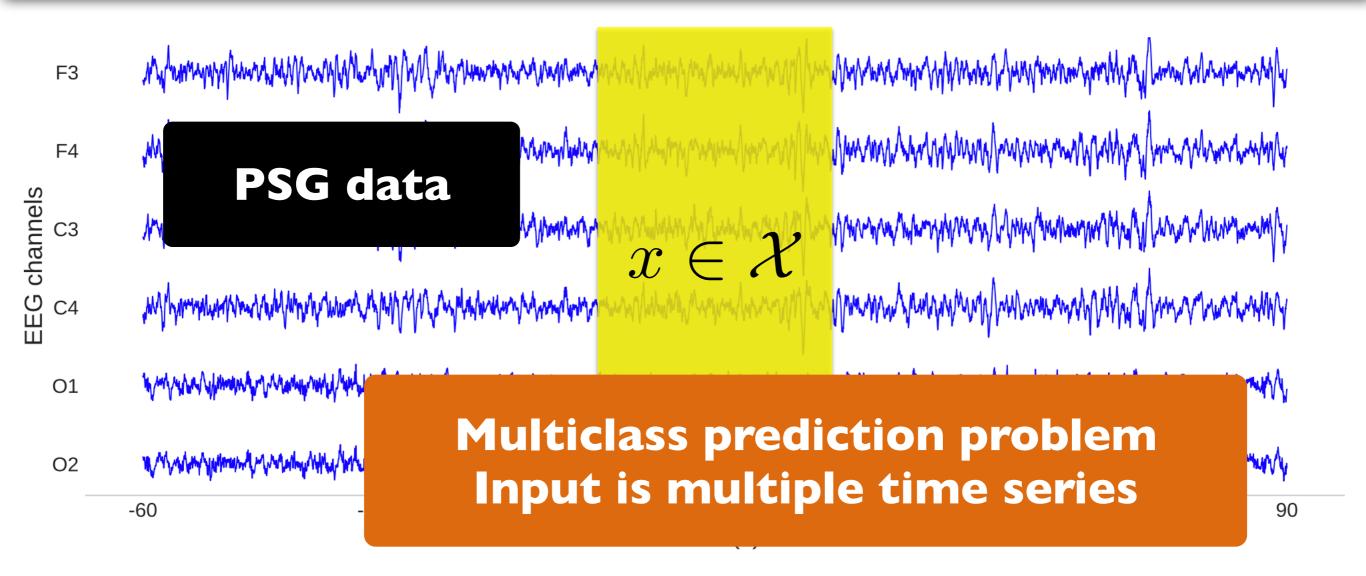






Learn:
$$\hat{f}:\mathcal{X} o \mathcal{Y}$$

 $\mathcal{Y} = \{\text{Awake, REM, Stage 1, Stage 2, etc.}\}$



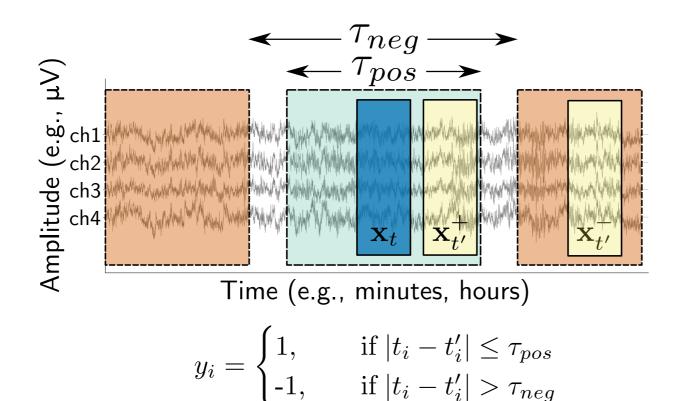
Learn:
$$\hat{f}:\mathcal{X} \to \mathcal{Y}$$

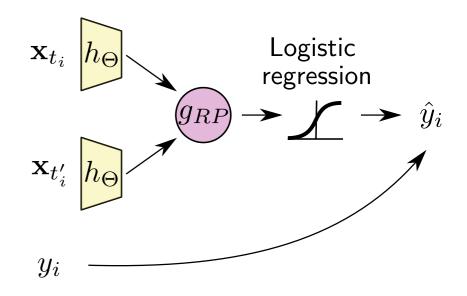
 $\mathcal{Y} = \{Awake, REM, Stage 1, Stage 2, etc.\}$

Pretext Task

Relative positioning (RP)

1 Sampling







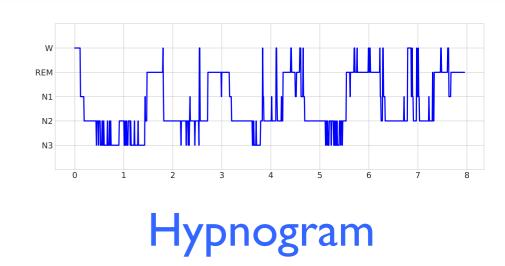
Predict if 2 windows of data are close in time

Related to PCL [Hyvärinen et al. 2017]

Downstream tasks on clinical EEG

Sleep staging:

Predict sleep stage from EEG (5-class: W, N1, N2, N3, R)

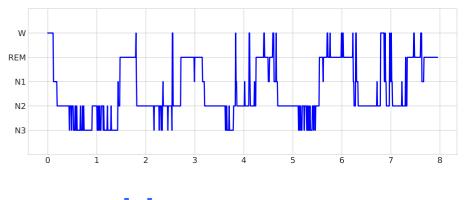


Dataset: Physionet Challenge 2018 (PC18) [Ghassemi et al. 2018]

Downstream tasks on clinical EEG

Sleep staging:

Predict sleep stage from EEG (5-class: W, N1, N2, N3, R)



Hypnogram

Dataset: Physionet Challenge 2018 (PC18) [Ghassemi et al. 2018]

Pathology detection:

Is someone's EEG pathological? (2-class: normal, abnormal)



Dataset: TUH Abnormal EEG (TUHab) [López 2017]

Datasets

Two public datasets with hundreds of recordings:

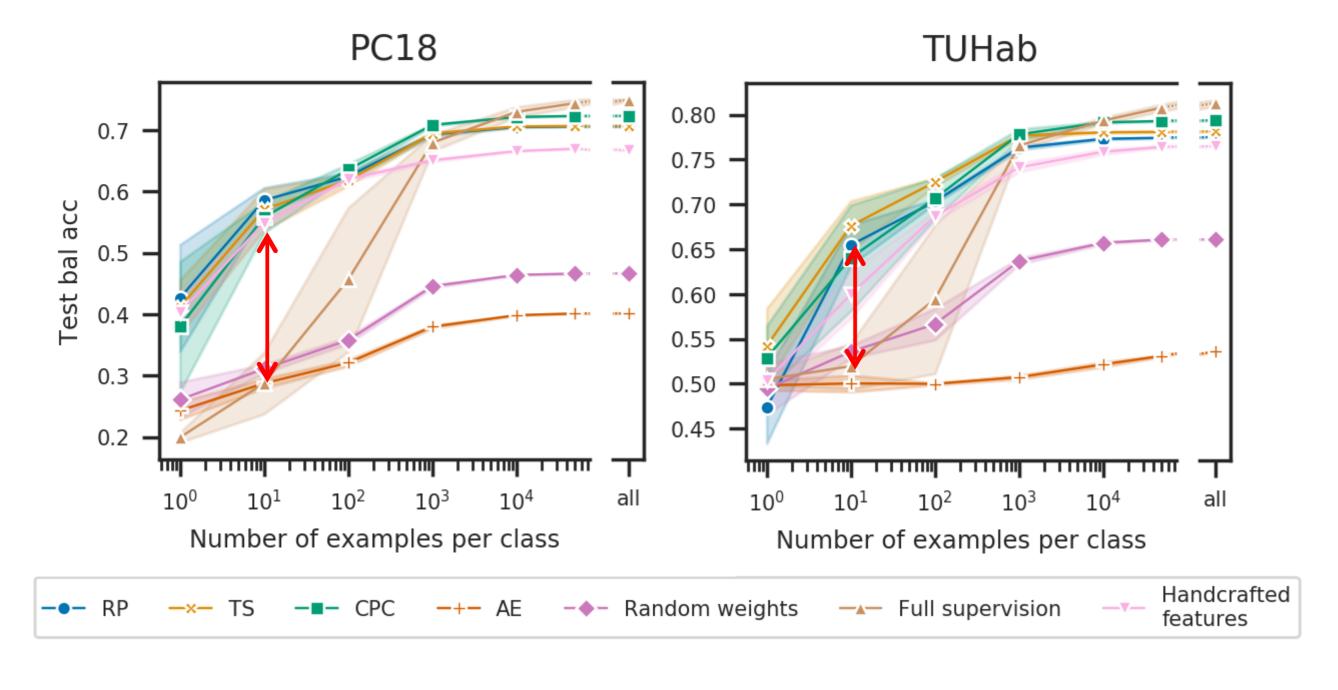
- Sleep staging: Physionet Challenge 2018 (PC18) [Ghassemi et al. 2018]
- Pathology detection: TUH Abnormal EEG (TUHab) [López 2017]

	PC18 (train)	
	# windows	
\mathbf{W}	158,020	
N1	$136,\!858$	
N2	$377,\!426$	
N3	102,492	
R	116,872	
Total	891,668	
# unique subjects	994	
# recordings	994	
Sampling frequency	$200~\mathrm{Hz}$	
# EEG channels	6	
Reference	M1 or M2	

	TUHab (train)	TUHab (eval)
	# recordings	# recordings
Normal	1371	150
Abnormal	1346	126
Total	2717	276
# unique subjects # recordings Sampling frequency # EEG channels	2329 2993 250, 256, 512 Hz 27 to 36	
Reference	Common	average

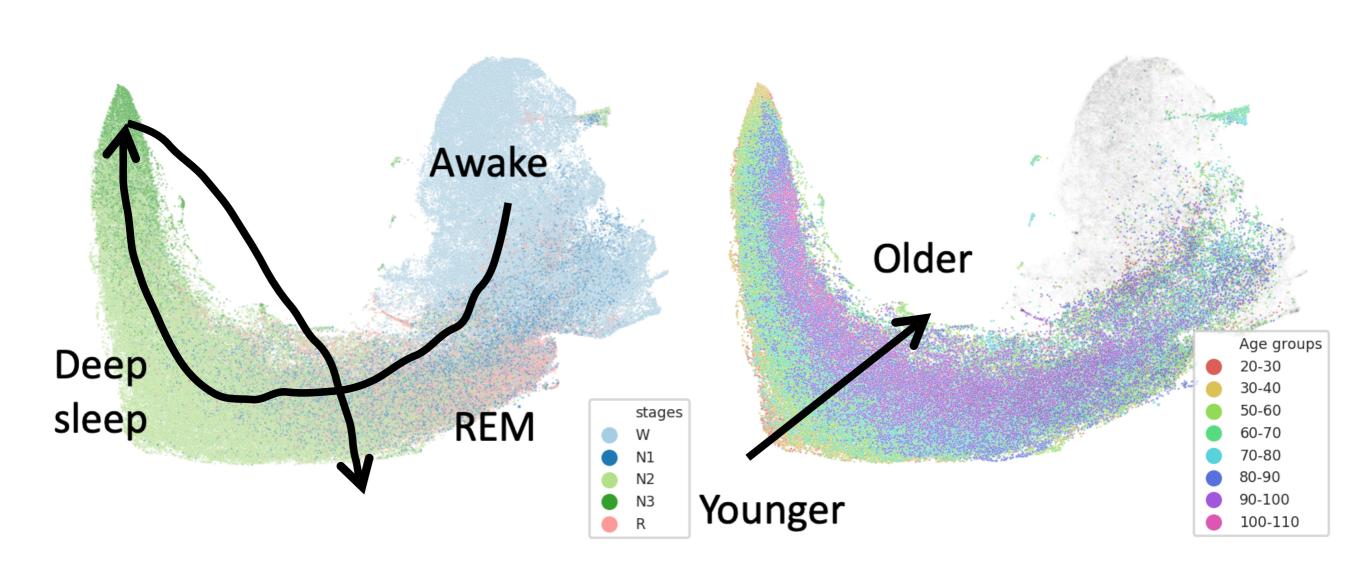
Results: Prediction accuracy

Using a CNN (2 conv/relu/mp) layers described in [Chambon et al. 2017]



SSL is **better than full supervision** when limited data is available, and **competitive** when all data is available.

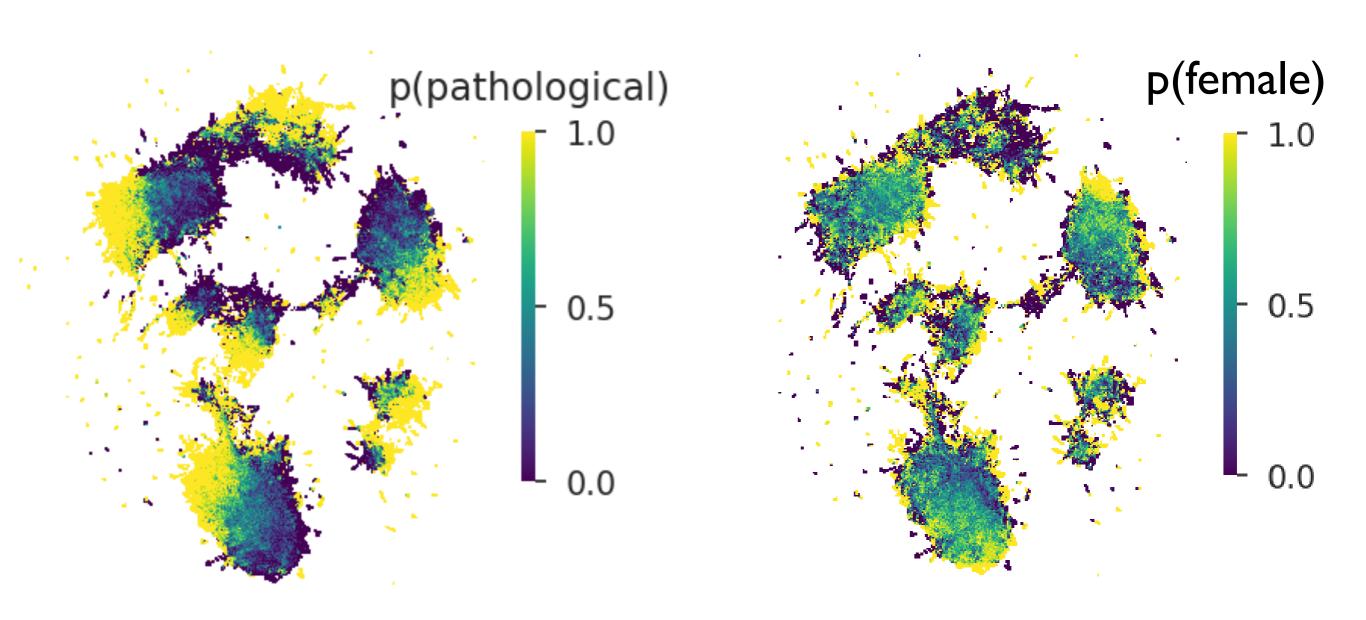
Results on sleep EEG



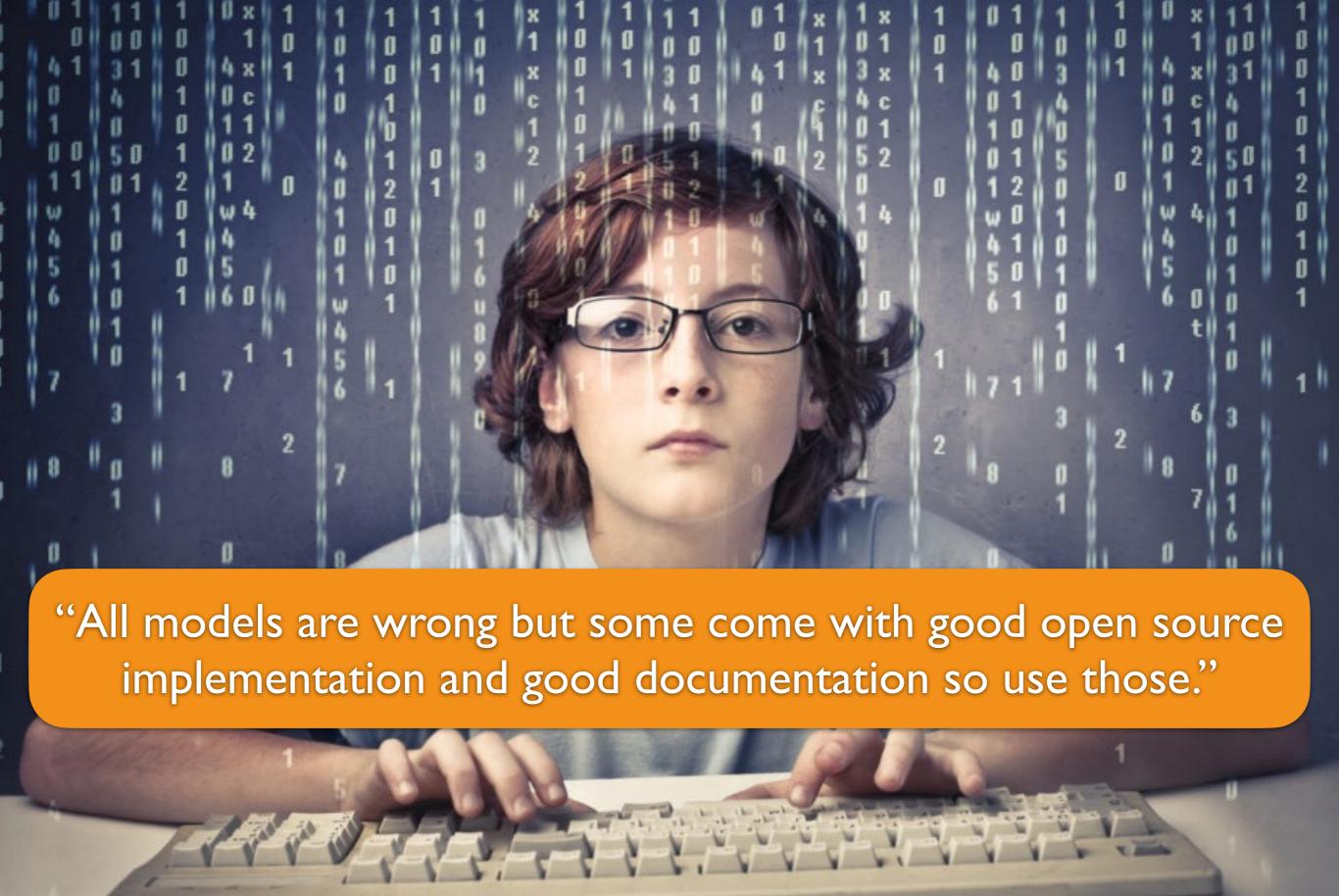
SSL can uncover structure without human supervision

[Banville et al. MLSP 2019]

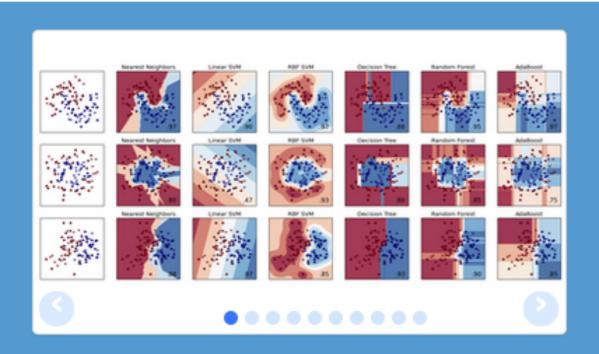
Results on TUH data



SSL can uncover clinically-relevant structure without human supervision







Examples

scikit-learn

Machine Learning in Python

- Simple and efficient tools for data mining and data analysis
- Accessible to everybody, and reusable in various contexts
- Built on NumPy, SciPy, and matplotlib
- Open source, commercially usable BSD license

Classification

Identifying to which category an object belongs to.

learn

Applications: Spam detection, Image recognition.

Algorithms: SVM, nearest neighbors,

random forest, ...

Regression

Predicting a continuous-valued attribute associated with an object.

Applications: Drug response, Stock prices. Algorithms: SVR, ridge regression, Lasso,

— Examples

Clustering

Automatic grouping of similar objects into sets.

Applications: Customer segmentation, Grouping experiment outcomes

Algorithms: k-Means, spectral clustering,

mean-shift, ... – Examples

Dimensionality reduction

Reducing the number of random variables to consider.

Applications: Visualization, Increased efficiency

Algorithms: PCA feature selection non-

Model selection

Comparing, validating and choosing parameters and models.

Goal: Improved accuracy via parameter tuning

Modules: arid search, cross validation

Preprocessing

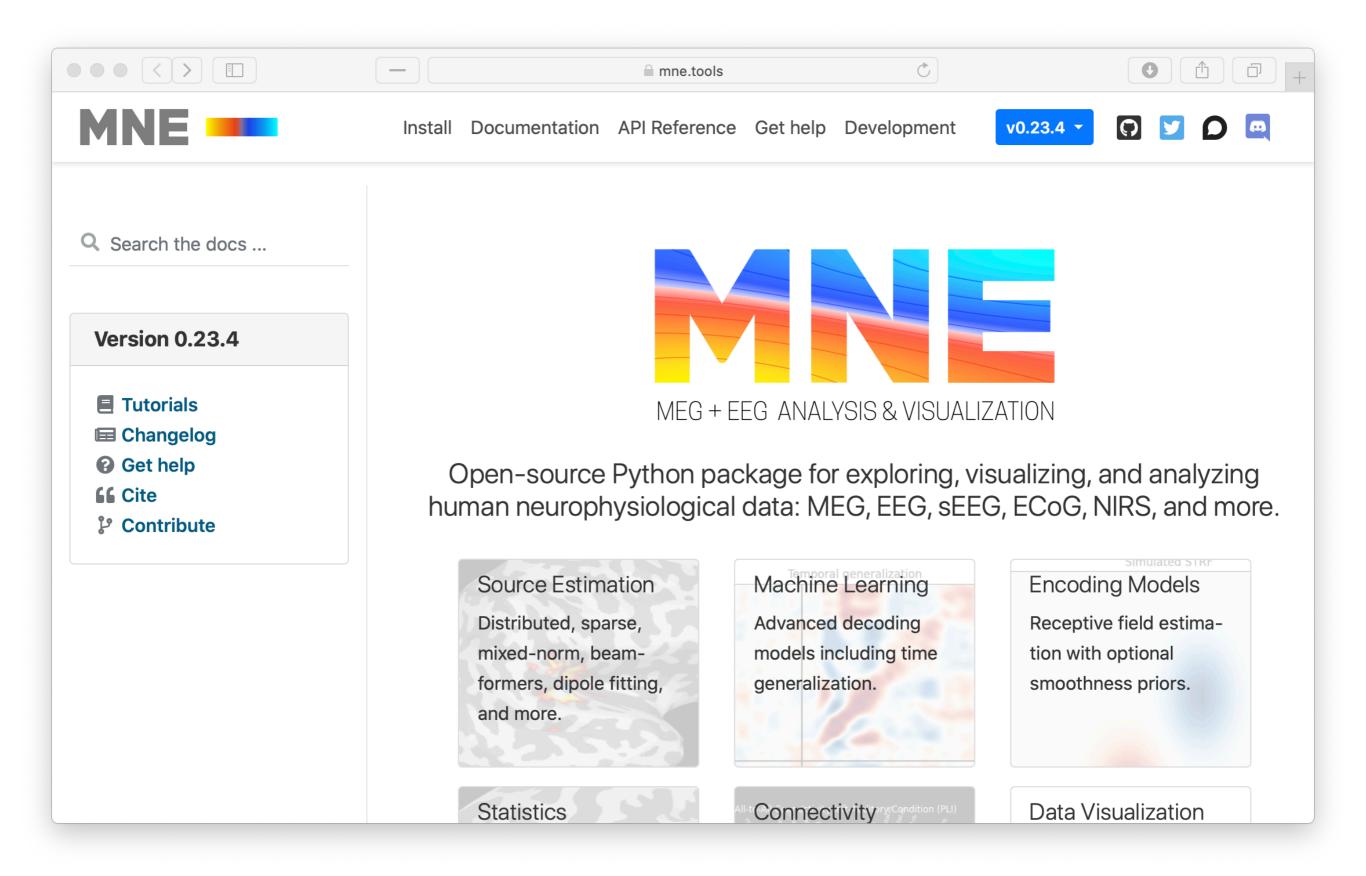
Feature extraction and normalization.

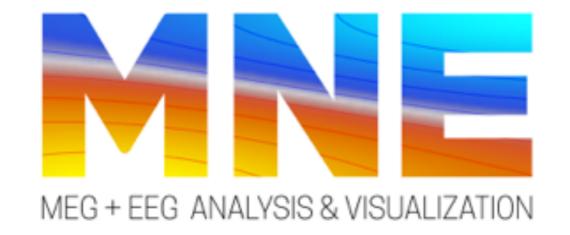
Application: Transforming input data such as text for use with machine learning algorithms.

Modules: preprocessing, feature extraction.

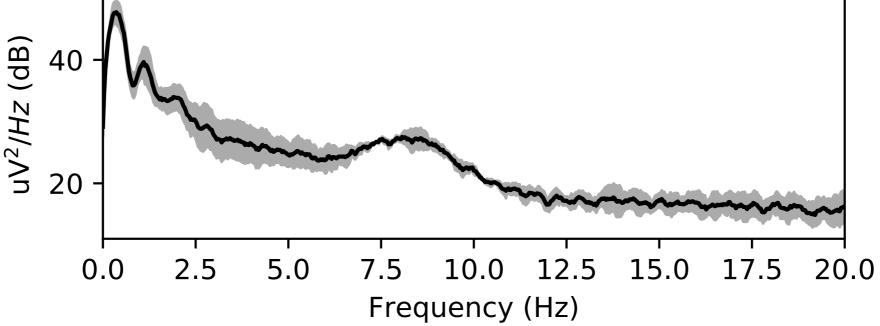
http://scikit-learn.org

http://mne.tools



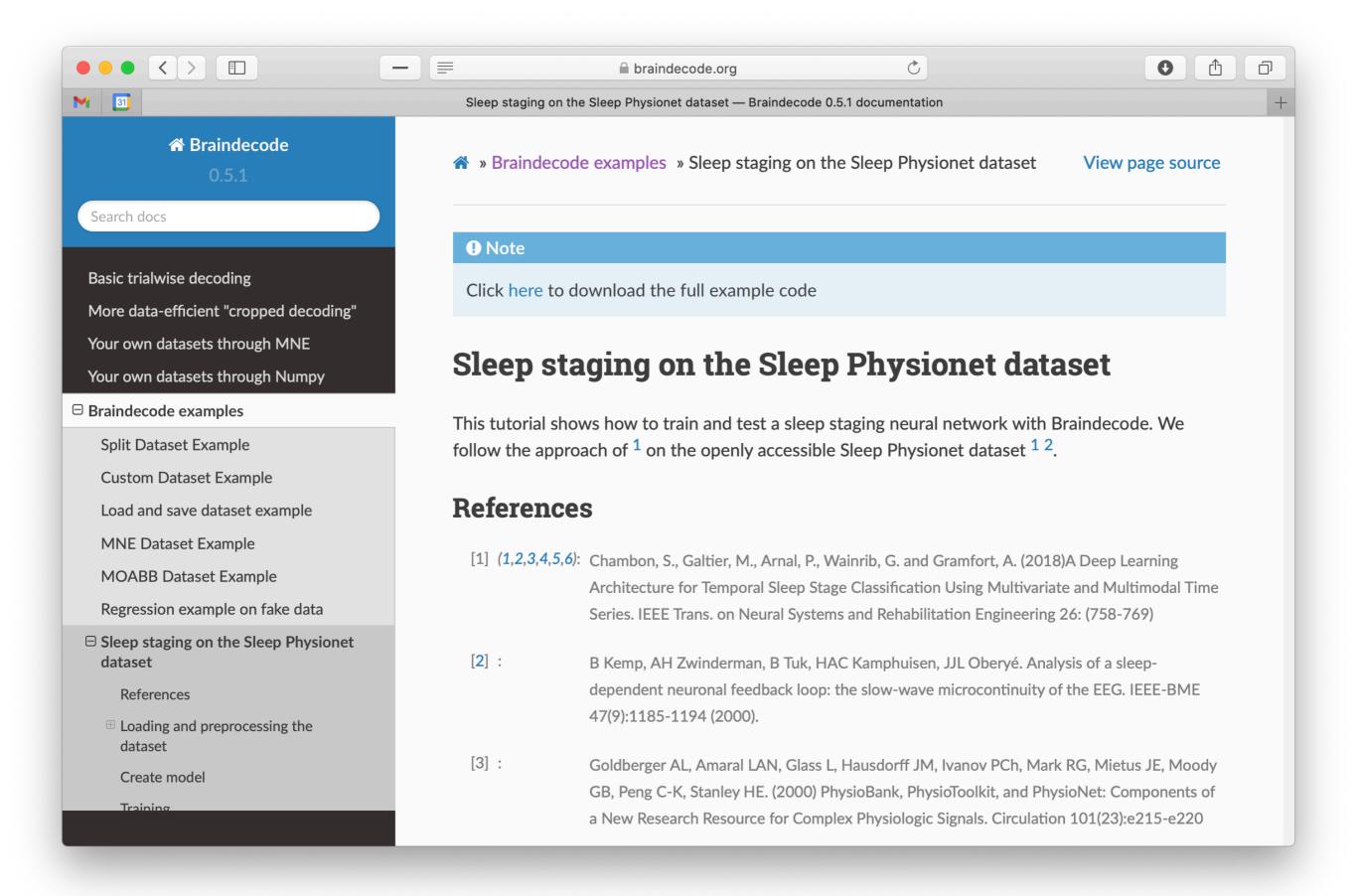


Working with EEG sleep data in 7 lines of Python code

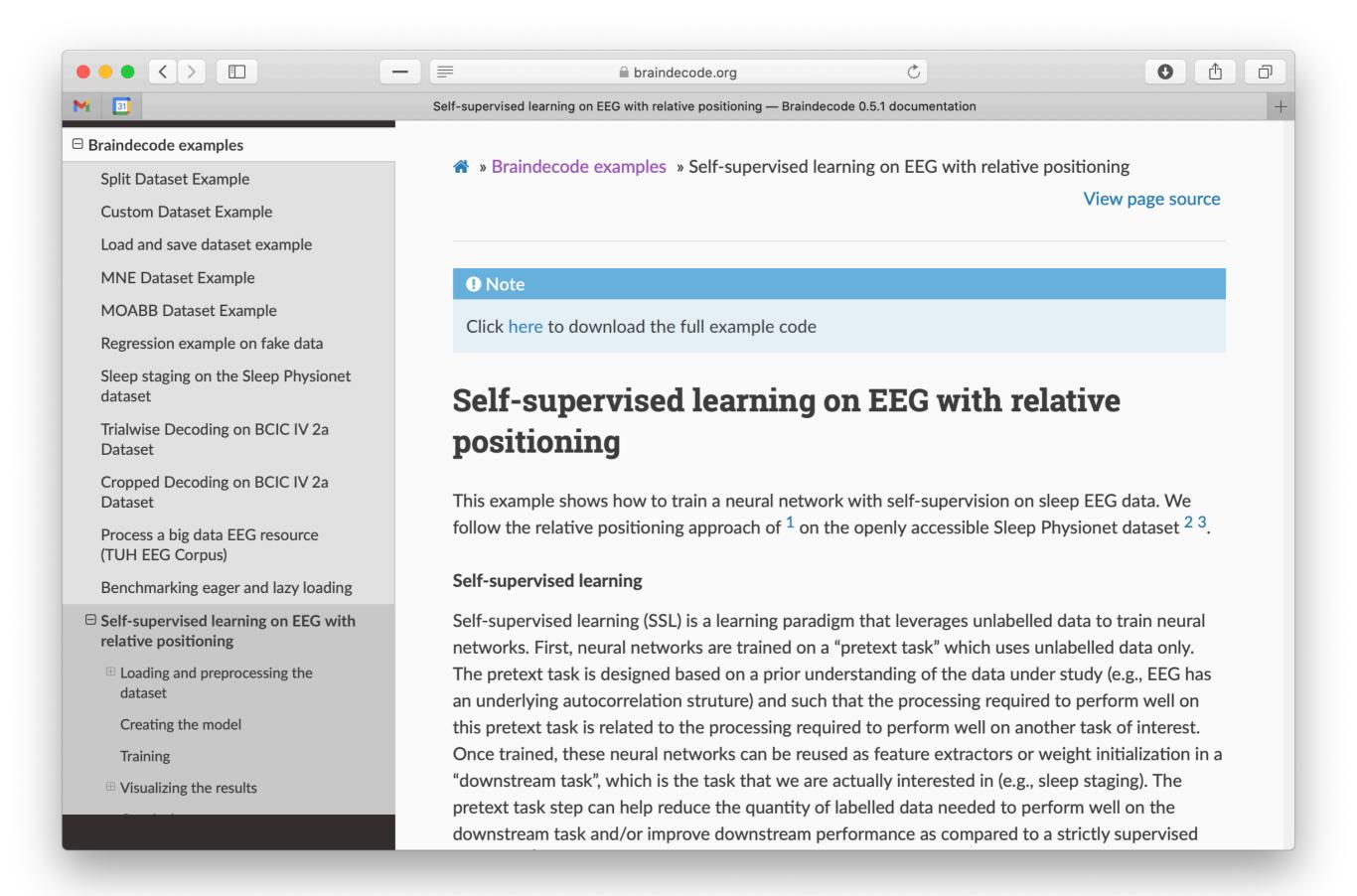


https://mne.tools/stable/auto tutorials/clinical/60 sleep.html

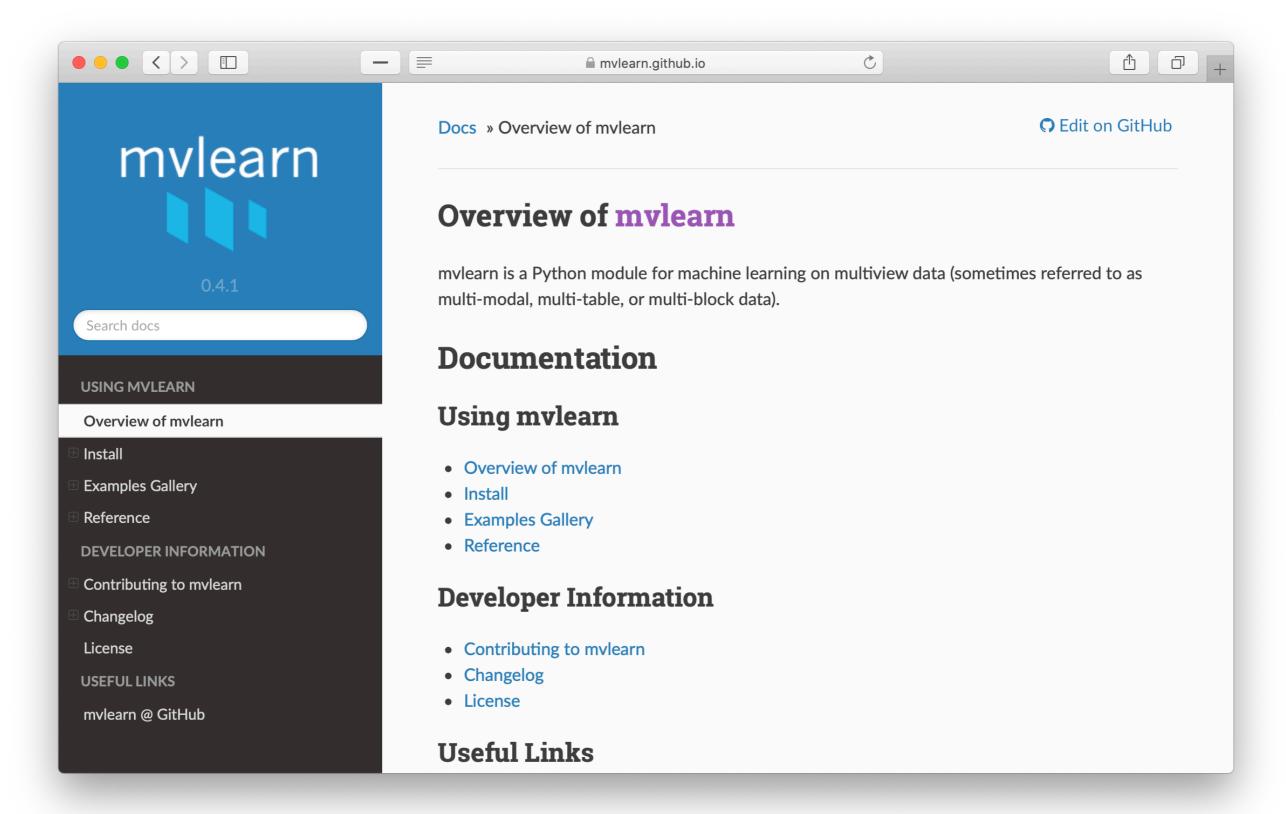
https://braindecode.org



https://braindecode.org



https://mvlearn.github.io



[Perry, Ronan, et al. "mvlearn: Multiview Machine Learning in Python." Journal of Machine Learning Research 22.109 (2021): 1-7.]

Thanks!

P. Ablin, J-F Cardoso, A. Gramfort (2017), Faster independent component analysis by preconditioning with Hessian approximations, IEEE Trans. Sig. Proc.

Richard, H., Gresele, L., Hyvärinen, A., Thirion, B., Gramfort, A., Ablin, P. (2020), Modeling Shared Responses in Neuroimaging Studies through MultiView ICA, Proc. NeurIPS

Richard, H., Ablin, P., Thirion, B., Gramfort, A., Hyvärinen, A., P. (2021), Shared Independent Component Analysis for Multi-Subject Neuroimaging, Proc. NeurIPS

Banville, H., Chehab, O., Hyvärinen, A., Engemann, D. and Gramfort, A. (2020), Uncovering the structure of clinical EEG signals with self-supervised learning, J. Neural Engineering

Contact

http://alexandre.gramfort.net



GitHub: @agramfort Twitter: @agramfort





Support

ERC SLAB, ANR-14-NEUC-0002-01 NIH R01 MH106174, ANR AI Chaire BrAIN, ANR AI-Cog